

Maple 2018.2 Integration Test Results  
on the problems in "4 Trig functions/4.4 Cotangent"

Test results for the 17 problems in "4.4.0 (a trig)^m (b cot)^n.txt"

Problem 10: Unable to integrate problem.

$$\int \cot(bx + a)^n dx$$

Optimal(type 5, 44 leaves, 2 steps):

$$-\frac{\cot(bx + a)^{1+n} \operatorname{hypergeom}\left(\left[1, \frac{1}{2} + \frac{n}{2}\right], \left[\frac{3}{2} + \frac{n}{2}\right], -\cot(bx + a)^2\right)}{b(1+n)}$$

Result(type 8, 10 leaves):

$$\int \cot(bx + a)^n dx$$

Problem 13: Unable to integrate problem.

$$\int (b \cot(fx + e))^n (a \sin(fx + e))^m dx$$

Optimal(type 5, 81 leaves, 2 steps):

$$-\frac{(b \cot(fx + e))^{1+n} \operatorname{hypergeom}\left(\left[\frac{1}{2} + \frac{n}{2}, \frac{1}{2} - \frac{m}{2} + \frac{n}{2}\right], \left[\frac{3}{2} + \frac{n}{2}\right], \cos(fx + e)^2\right) (a \sin(fx + e))^m (\sin(fx + e)^2)^{\frac{1}{2} - \frac{m}{2} + \frac{n}{2}}}{bf(1+n)}$$

Result(type 8, 23 leaves):

$$\int (b \cot(fx + e))^n (a \sin(fx + e))^m dx$$

Problem 14: Unable to integrate problem.

$$\int (a \cot(fx + e))^m (b \cot(fx + e))^n dx$$

Optimal(type 5, 66 leaves, 3 steps):

$$-\frac{(a \cot(fx + e))^{1+m} (b \cot(fx + e))^n \operatorname{hypergeom}\left(\left[1, \frac{1}{2} + \frac{m}{2} + \frac{n}{2}\right], \left[\frac{3}{2} + \frac{m}{2} + \frac{n}{2}\right], -\cot(fx + e)^2\right)}{af(1+m+n)}$$

Result(type 8, 23 leaves):

$$\int (a \cot(fx + e))^m (b \cot(fx + e))^n dx$$

Problem 16: Unable to integrate problem.

$$\int (d \cot(fx + e))^n \sin(fx + e)^4 dx$$

Optimal(type 5, 49 leaves, 2 steps):

$$\frac{(d \cot(fx + e))^{1+n} \text{hypergeom}\left(\left[3, \frac{1}{2} + \frac{n}{2}\right], \left[\frac{3}{2} + \frac{n}{2}\right], -\cot(fx + e)^2\right)}{df(1+n)}$$

Result(type 8, 21 leaves):

$$\int (d \cot(fx + e))^n \sin(fx + e)^4 dx$$

Problem 17: Unable to integrate problem.

$$\int (d \cot(fx + e))^n \csc(fx + e) dx$$

Optimal(type 5, 71 leaves, 1 step):

$$\frac{(d \cot(fx + e))^{1+n} \csc(fx + e) \text{hypergeom}\left(\left[1 + \frac{n}{2}, \frac{1}{2} + \frac{n}{2}\right], \left[\frac{3}{2} + \frac{n}{2}\right], \cos(fx + e)^2\right) (\sin(fx + e)^2)^{1+\frac{n}{2}}}{df(1+n)}$$

Result(type 8, 19 leaves):

$$\int (d \cot(fx + e))^n \csc(fx + e) dx$$

Test results for the 10 problems in "4.4.1.2 (d csc)^m (a+b cot)^n.txt"

Problem 3: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc(x)^3}{1 + \cot(x)} dx$$

Optimal(type 3, 11 leaves, 2 steps):

$$1 \arctanh(\cos(x)) - \csc(x)$$

Result(type 3, 23 leaves):

$$-\frac{\tan\left(\frac{x}{2}\right)}{2} - \ln\left(\tan\left(\frac{x}{2}\right)\right) - \frac{1}{2 \tan\left(\frac{x}{2}\right)}$$

Problem 5: Result more than twice size of optimal antiderivative.

$$\int \frac{\sin(x)^2}{a + b \cot(x)} dx$$

Optimal(type 3, 68 leaves, 7 steps):

$$\frac{a(a^2 + 3b^2)x}{2(a^2 + b^2)^2} - \frac{b^3 \ln(b \cos(x) + a \sin(x))}{(a^2 + b^2)^2} - \frac{(b + a \cot(x)) \sin(x)^2}{2(a^2 + b^2)}$$

Result(type 3, 172 leaves):

$$-\frac{\tan(x) a^3}{2(a^2 + b^2)^2 (\tan(x)^2 + 1)} - \frac{\tan(x) a b^2}{2(a^2 + b^2)^2 (\tan(x)^2 + 1)} + \frac{a^2 b}{2(a^2 + b^2)^2 (\tan(x)^2 + 1)} + \frac{b^3}{2(a^2 + b^2)^2 (\tan(x)^2 + 1)} + \frac{b^3 \ln(\tan(x)^2 + 1)}{2(a^2 + b^2)^2}$$

$$+ \frac{3 \arctan(\tan(x)) a b^2}{2(a^2 + b^2)^2} + \frac{\arctan(\tan(x)) a^3}{2(a^2 + b^2)^2} - \frac{b^3 \ln(a \tan(x) + b)}{(a^2 + b^2)^2}$$

Problem 6: Result more than twice size of optimal antiderivative.

$$\int \frac{\sin(x)^4}{a + b \cot(x)} dx$$

Optimal(type 3, 114 leaves, 8 steps):

$$\frac{a(3a^4 + 10a^2b^2 + 15b^4)x}{8(a^2 + b^2)^3} - \frac{b^5 \ln(b \cos(x) + a \sin(x))}{(a^2 + b^2)^3} - \frac{(4b^3 + a(3a^2 + 7b^2) \cot(x)) \sin(x)^2}{8(a^2 + b^2)^2} - \frac{(b + a \cot(x)) \sin(x)^4}{4(a^2 + b^2)}$$

Result(type 3, 406 leaves):

$$-\frac{7 \tan(x)^3 a^3 b^2}{4(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} - \frac{9 \tan(x)^3 a b^4}{8(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} - \frac{5 \tan(x)^3 a^5}{8(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} + \frac{\tan(x)^2 a^4 b}{2(a^2 + b^2)^3 (\tan(x)^2 + 1)^2}$$

$$+ \frac{3 \tan(x)^2 a^2 b^3}{2(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} + \frac{\tan(x)^2 b^5}{(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} - \frac{3 \tan(x) a^5}{8(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} - \frac{5 \tan(x) a^3 b^2}{4(a^2 + b^2)^3 (\tan(x)^2 + 1)^2}$$

$$- \frac{7 \tan(x) a b^4}{8(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} + \frac{a^4 b}{4(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} + \frac{a^2 b^3}{(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} + \frac{3 b^5}{4(a^2 + b^2)^3 (\tan(x)^2 + 1)^2} + \frac{b^5 \ln(\tan(x)^2 + 1)}{2(a^2 + b^2)^3}$$

$$+ \frac{15 \arctan(\tan(x)) a b^4}{8(a^2 + b^2)^3} + \frac{3 \arctan(\tan(x)) a^5}{8(a^2 + b^2)^3} + \frac{5 \arctan(\tan(x)) a^3 b^2}{4(a^2 + b^2)^3} - \frac{b^5 \ln(a \tan(x) + b)}{(a^2 + b^2)^3}$$

Problem 7: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc(x)^5}{a + b \cot(x)} dx$$

Optimal(type 3, 91 leaves, 9 steps):

$$\frac{a \operatorname{arctanh}(\cos(x))}{2b^2} + \frac{a(a^2 + b^2) \operatorname{arctanh}(\cos(x))}{b^4} + \frac{(a^2 + b^2)^{3/2} \operatorname{arctanh}\left(\frac{(b - a \cot(x)) \sin(x)}{\sqrt{a^2 + b^2}}\right)}{b^4} - \frac{(a^2 + b^2) \csc(x)}{b^3} + \frac{a \cot(x) \csc(x)}{2b^2} - \frac{\csc(x)^3}{3b}$$

Result(type 3, 231 leaves):

$$\begin{aligned}
& -\frac{\tan\left(\frac{x}{2}\right)^3}{24b} - \frac{a \tan\left(\frac{x}{2}\right)^2}{8b^2} - \frac{a^2 \tan\left(\frac{x}{2}\right)}{2b^3} - \frac{5 \tan\left(\frac{x}{2}\right)}{8b} - \frac{1}{24b \tan\left(\frac{x}{2}\right)^3} - \frac{a^2}{2b^3 \tan\left(\frac{x}{2}\right)} - \frac{5}{8b \tan\left(\frac{x}{2}\right)} + \frac{a}{8b^2 \tan\left(\frac{x}{2}\right)^2} - \frac{a^3 \ln\left(\tan\left(\frac{x}{2}\right)\right)}{b^4} \\
& - \frac{3a \ln\left(\tan\left(\frac{x}{2}\right)\right)}{2b^2} + \frac{2 \operatorname{arctanh}\left(\frac{2 \tan\left(\frac{x}{2}\right)b - 2a}{2\sqrt{a^2 + b^2}}\right) a^4}{b^4 \sqrt{a^2 + b^2}} + \frac{4 \operatorname{arctanh}\left(\frac{2 \tan\left(\frac{x}{2}\right)b - 2a}{2\sqrt{a^2 + b^2}}\right) a^2}{b^2 \sqrt{a^2 + b^2}} + \frac{2 \operatorname{arctanh}\left(\frac{2 \tan\left(\frac{x}{2}\right)b - 2a}{2\sqrt{a^2 + b^2}}\right)}{\sqrt{a^2 + b^2}}
\end{aligned}$$

Problem 8: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc(x)^3}{a + b \cot(x)} dx$$

Optimal(type 3, 49 leaves, 5 steps):

$$\frac{a \operatorname{arctanh}(\cos(x))}{b^2} - \frac{\csc(x)}{b} + \frac{\operatorname{arctanh}\left(\frac{(b - a \cot(x)) \sin(x)}{\sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2}$$

Result(type 3, 106 leaves):

$$-\frac{\tan\left(\frac{x}{2}\right)}{2b} - \frac{1}{2b \tan\left(\frac{x}{2}\right)} - \frac{a \ln\left(\tan\left(\frac{x}{2}\right)\right)}{b^2} + \frac{2 \operatorname{arctanh}\left(\frac{2 \tan\left(\frac{x}{2}\right)b - 2a}{2\sqrt{a^2 + b^2}}\right) a^2}{b^2 \sqrt{a^2 + b^2}} + \frac{2 \operatorname{arctanh}\left(\frac{2 \tan\left(\frac{x}{2}\right)b - 2a}{2\sqrt{a^2 + b^2}}\right)}{\sqrt{a^2 + b^2}}$$

Test results for the 9 problems in "4.4.1.3 (d cos)^m (a+b cot)^n.txt"

Problem 3: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec(x)^3}{1 + \cot(x)} dx$$

Optimal(type 3, 16 leaves, 8 steps):

$$\frac{\operatorname{Iarctanh}(\sin(x))}{2} + \sec(x) - \frac{\operatorname{Isec}(x) \tan(x)}{2}$$

Result(type 3, 83 leaves):

$$\frac{\operatorname{I}}{2 \left(\tan\left(\frac{x}{2}\right) + 1\right)^2} + \frac{\operatorname{I} \ln\left(\tan\left(\frac{x}{2}\right) + 1\right)}{2} + \frac{1}{\tan\left(\frac{x}{2}\right) + 1} - \frac{\operatorname{I}}{2 \left(\tan\left(\frac{x}{2}\right) + 1\right)} - \frac{\operatorname{I} \ln\left(\tan\left(\frac{x}{2}\right) - 1\right)}{2} - \frac{\operatorname{I}}{2 \left(\tan\left(\frac{x}{2}\right) - 1\right)^2} - \frac{1}{\tan\left(\frac{x}{2}\right) - 1}$$

$$-\frac{1}{2 \left( \tan\left(\frac{x}{2}\right) - 1 \right)}$$

Problem 7: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec(x)^3}{a + b \cot(x)} dx$$

Optimal(type 3, 71 leaves, 9 steps):

$$\frac{\operatorname{arctanh}(\sin(x))}{2a} + \frac{b^2 \operatorname{arctanh}(\sin(x))}{a^3} - \frac{b \sec(x)}{a^2} + \frac{b \operatorname{arctanh}\left(\frac{\cos(x)a - \sin(x)b}{\sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a^3} + \frac{\sec(x) \tan(x)}{2a}$$

Result(type 3, 171 leaves):

$$\begin{aligned} & -\frac{1}{2a \left( \tan\left(\frac{x}{2}\right) + 1 \right)^2} + \frac{1}{2a \left( \tan\left(\frac{x}{2}\right) + 1 \right)} - \frac{b}{a^2 \left( \tan\left(\frac{x}{2}\right) + 1 \right)} + \frac{\ln\left(\tan\left(\frac{x}{2}\right) + 1\right)}{2a} + \frac{\ln\left(\tan\left(\frac{x}{2}\right) + 1\right) b^2}{a^3} + \frac{1}{2a \left( \tan\left(\frac{x}{2}\right) - 1 \right)^2} \\ & + \frac{1}{2a \left( \tan\left(\frac{x}{2}\right) - 1 \right)} + \frac{b}{a^2 \left( \tan\left(\frac{x}{2}\right) - 1 \right)} - \frac{\ln\left(\tan\left(\frac{x}{2}\right) - 1\right)}{2a} - \frac{\ln\left(\tan\left(\frac{x}{2}\right) - 1\right) b^2}{a^3} - \frac{2b\sqrt{a^2 + b^2} \operatorname{arctanh}\left(\frac{2 \tan\left(\frac{x}{2}\right) b - 2a}{2\sqrt{a^2 + b^2}}\right)}{a^3} \end{aligned}$$

Test results for the 19 problems in "4.4.10 (c+d x)^m (a+b cot)^n.txt"

Problem 1: Result more than twice size of optimal antiderivative.

$$\int x^3 \cot(bx + a) dx$$

Optimal(type 4, 82 leaves, 6 steps):

$$-\frac{Ix^4}{4} + \frac{x^3 \ln(1 - e^{2I(bx+a)})}{b} - \frac{3Ix^2 \operatorname{polylog}(2, e^{2I(bx+a)})}{2b^2} + \frac{3x \operatorname{polylog}(3, e^{2I(bx+a)})}{2b^3} + \frac{3I \operatorname{polylog}(4, e^{2I(bx+a)})}{4b^4}$$

Result(type 4, 239 leaves):

$$\begin{aligned} & -\frac{Ix^4}{4} + \frac{\ln(e^{I(bx+a)} + 1) x^3}{b} + \frac{\ln(1 - e^{I(bx+a)}) x^3}{b} + \frac{\ln(1 - e^{I(bx+a)}) a^3}{b^4} - \frac{3I \operatorname{polylog}(2, e^{I(bx+a)}) x^2}{b^2} - \frac{3I \operatorname{polylog}(2, -e^{I(bx+a)}) x^2}{b^2} - \frac{2Ia^3 x}{b^3} \\ & - \frac{a^3 \ln(e^{I(bx+a)} - 1)}{b^4} + \frac{2a^3 \ln(e^{I(bx+a)})}{b^4} - \frac{3Ia^4}{2b^4} + \frac{6I \operatorname{polylog}(4, -e^{I(bx+a)})}{b^4} + \frac{6I \operatorname{polylog}(4, e^{I(bx+a)})}{b^4} + \frac{6 \operatorname{polylog}(3, -e^{I(bx+a)}) x}{b^3} \\ & + \frac{6 \operatorname{polylog}(3, e^{I(bx+a)}) x}{b^3} \end{aligned}$$

Problem 2: Result more than twice size of optimal antiderivative.

$$\int x \cot(bx + a) dx$$

Optimal(type 4, 43 leaves, 4 steps):

$$-\frac{Ix^2}{2} + \frac{x \ln(1 - e^{2I(bx+a)})}{b} - \frac{I \text{polylog}(2, e^{2I(bx+a)})}{2b^2}$$

Result(type 4, 149 leaves):

$$\begin{aligned} &-\frac{Ix^2}{2} - \frac{2Iax}{b} - \frac{Ia^2}{b^2} + \frac{\ln(1 - e^{I(bx+a)})x}{b} + \frac{a \ln(1 - e^{I(bx+a)})}{b^2} - \frac{I \text{polylog}(2, e^{I(bx+a)})}{b^2} + \frac{\ln(e^{I(bx+a)} + 1)x}{b} - \frac{I \text{polylog}(2, -e^{I(bx+a)})}{b^2} \\ &+ \frac{2a \ln(e^{I(bx+a)})}{b^2} - \frac{a \ln(e^{I(bx+a)} - 1)}{b^2} \end{aligned}$$

Problem 3: Result more than twice size of optimal antiderivative.

$$\int x^2 \cot(bx + a)^2 dx$$

Optimal(type 4, 66 leaves, 6 steps):

$$-\frac{Ix^2}{b} - \frac{x^3}{3} - \frac{x^2 \cot(bx + a)}{b} + \frac{2x \ln(1 - e^{2I(bx+a)})}{b^2} - \frac{I \text{polylog}(2, e^{2I(bx+a)})}{b^3}$$

Result(type 4, 182 leaves):

$$\begin{aligned} &-\frac{x^3}{3} - \frac{2Ix^2}{b(e^{2I(bx+a)} - 1)} - \frac{2Ix^2}{b} - \frac{4Iax}{b^2} - \frac{2Ia^2}{b^3} + \frac{2 \ln(1 - e^{I(bx+a)})x}{b^2} + \frac{2a \ln(1 - e^{I(bx+a)})}{b^3} - \frac{2I \text{polylog}(2, e^{I(bx+a)})}{b^3} + \frac{2 \ln(e^{I(bx+a)} + 1)x}{b^2} \\ &- \frac{2I \text{polylog}(2, -e^{I(bx+a)})}{b^3} + \frac{4a \ln(e^{I(bx+a)})}{b^3} - \frac{2a \ln(e^{I(bx+a)} - 1)}{b^3} \end{aligned}$$

Problem 10: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx + c)^2}{(a + Ia \cot(fx + e))^2} dx$$

Optimal(type 3, 166 leaves, 8 steps):

$$-\frac{Id^2 e^{2Ie+2Ifx}}{8a^2 f^3} + \frac{Id^2 e^{4Ie+4Ifx}}{128a^2 f^3} - \frac{de^{2Ie+2Ifx}(dx + c)}{4a^2 f^2} + \frac{de^{4Ie+4Ifx}(dx + c)}{32a^2 f^2} + \frac{Ie^{2Ie+2Ifx}(dx + c)^2}{4a^2 f} - \frac{Ie^{4Ie+4Ifx}(dx + c)^2}{16a^2 f} + \frac{(dx + c)^3}{12a^2 d}$$

Result(type 3, 1042 leaves):

$$-\frac{1}{f^3 a^2} \left( -Icdef \sin(fx + e)^4 + 4Icdf \left( \frac{(fx + e) \sin(fx + e)^4}{4} + \frac{(\sin(fx + e)^3 + \frac{3 \sin(fx + e)}{2}) \cos(fx + e)}{16} - \frac{3fx}{32} - \frac{3e}{32} \right) + \frac{Ic^2 f^2 \sin(fx + e)^4}{2} \right)$$

$$\begin{aligned}
& + 2 I d^2 \left( \frac{(fx+e)^2 \sin(fx+e)^4}{4} - \frac{(fx+e) \left( -\frac{\left( \sin(fx+e)^3 + \frac{3 \sin(fx+e)}{2} \right) \cos(fx+e)}{4} + \frac{3fx}{8} + \frac{3e}{8} \right)}{2} + \frac{3(fx+e)^2}{32} - \frac{\sin(fx+e)^4}{32} \right. \\
& \left. - \frac{3 \sin(fx+e)^2}{32} \right) + \frac{I d^2 e^2 \sin(fx+e)^4}{2} - 4 I d^2 e \left( \frac{(fx+e) \sin(fx+e)^4}{4} + \frac{\left( \sin(fx+e)^3 + \frac{3 \sin(fx+e)}{2} \right) \cos(fx+e)}{16} - \frac{3fx}{32} - \frac{3e}{32} \right) \\
& + 2 d^2 \left( (fx+e)^2 \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) - \frac{(fx+e) \cos(fx+e)^2}{8} + \frac{\cos(fx+e) \sin(fx+e)}{16} + \frac{7fx}{64} + \frac{7e}{64} - \frac{(fx+e)^3}{12} \right. \\
& - \frac{(fx+e)^2 \left( -\frac{\left( \sin(fx+e)^3 + \frac{3 \sin(fx+e)}{2} \right) \cos(fx+e)}{4} + \frac{3fx}{8} + \frac{3e}{8} \right) - \frac{(fx+e) \sin(fx+e)^4}{8}}{(fx+e)^2} \\
& \left. - \frac{\left( \sin(fx+e)^3 + \frac{3 \sin(fx+e)}{2} \right) \cos(fx+e)}{32} \right) + 4 c d f \left( (fx+e) \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) - \frac{(fx+e)^2}{16} + \frac{\sin(fx+e)^2}{16} - (fx \right. \\
& \left. + e) \left( -\frac{\left( \sin(fx+e)^3 + \frac{3 \sin(fx+e)}{2} \right) \cos(fx+e)}{4} + \frac{3fx}{8} + \frac{3e}{8} \right) - \frac{\sin(fx+e)^4}{16} \right) - 4 d^2 e \left( (fx+e) \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) \right. \\
& \left. - \frac{(fx+e)^2}{16} + \frac{\sin(fx+e)^2}{16} - (fx+e) \left( -\frac{\left( \sin(fx+e)^3 + \frac{3 \sin(fx+e)}{2} \right) \cos(fx+e)}{4} + \frac{3fx}{8} + \frac{3e}{8} \right) - \frac{\sin(fx+e)^4}{16} \right) + 2 c^2 f^2 \left( \right. \\
& \left. - \frac{\cos(fx+e)^3 \sin(fx+e)}{4} + \frac{\cos(fx+e) \sin(fx+e)}{8} + \frac{fx}{8} + \frac{e}{8} \right) - 4 c d e f \left( -\frac{\cos(fx+e)^3 \sin(fx+e)}{4} + \frac{\cos(fx+e) \sin(fx+e)}{8} + \frac{fx}{8} + \frac{e}{8} \right) \\
& + 2 d^2 e^2 \left( -\frac{\cos(fx+e)^3 \sin(fx+e)}{4} + \frac{\cos(fx+e) \sin(fx+e)}{8} + \frac{fx}{8} + \frac{e}{8} \right) - d^2 \left( (fx+e)^2 \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) \right. \\
& \left. - \frac{(fx+e) \cos(fx+e)^2}{2} + \frac{\cos(fx+e) \sin(fx+e)}{4} + \frac{fx}{4} + \frac{e}{4} - \frac{(fx+e)^3}{3} \right) - 2 c d f \left( (fx+e) \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) \right. \\
& \left. - \frac{(fx+e)^2}{4} + \frac{\sin(fx+e)^2}{4} \right) + 2 d^2 e \left( (fx+e) \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) - \frac{(fx+e)^2}{4} + \frac{\sin(fx+e)^2}{4} \right) - c^2 f^2 \left( \right. \\
& \left. - \frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) + 2 c d e f \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) - d^2 e^2 \left( -\frac{\cos(fx+e) \sin(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) \Big)
\end{aligned}$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int \frac{dx+c}{(a+Ia \cot(fx+e))^3} dx$$

Optimal(type 3, 181 leaves, 11 steps):

$$\frac{11 I d x}{96 a^3 f} - \frac{d x^2}{16 a^3} + \frac{x (d x + c)}{8 a^3} + \frac{d}{36 f^2 (a + I a \cot (f x + e))^3} - \frac{I (d x + c)}{6 f (a + I a \cot (f x + e))^3} + \frac{5 d}{96 a f^2 (a + I a \cot (f x + e))^2} - \frac{I (d x + c)}{8 a f (a + I a \cot (f x + e))^2}$$

$$+ \frac{11 d}{96 f^2 (a^3 + I a^3 \cot (f x + e))} - \frac{I (d x + c)}{8 f (a^3 + I a^3 \cot (f x + e))}$$

Result (type 3, 652 leaves):

$$\frac{1}{f^2 a^3} \left( 4 I d \left( \frac{(f x + e) \sin (f x + e)^4}{4} + \frac{\left( \sin (f x + e)^3 + \frac{3 \sin (f x + e)}{2} \right) \cos (f x + e)}{16} - \frac{f x}{24} - \frac{e}{24} - \frac{(f x + e) \sin (f x + e)^6}{6} \right. \right.$$

$$\left. - \frac{\left( \sin (f x + e)^5 + \frac{5 \sin (f x + e)^3}{4} + \frac{15 \sin (f x + e)}{8} \right) \cos (f x + e)}{36} \right) + 4 I c f \left( - \frac{\sin (f x + e)^2 \cos (f x + e)^4}{6} - \frac{\cos (f x + e)^4}{12} \right) - 4 I d e \left( \right.$$

$$\left. - \frac{\sin (f x + e)^2 \cos (f x + e)^4}{6} - \frac{\cos (f x + e)^4}{12} \right) - 4 d \left( (f x + e) \left( - \frac{\left( \sin (f x + e)^3 + \frac{3 \sin (f x + e)}{2} \right) \cos (f x + e)}{4} + \frac{3 f x}{8} + \frac{3 e}{8} \right) - \frac{(f x + e)^2}{32} \right.$$

$$\left. + \frac{\sin (f x + e)^4}{96} + \frac{\sin (f x + e)^2}{32} - (f x + e) \left( - \frac{\left( \sin (f x + e)^5 + \frac{5 \sin (f x + e)^3}{4} + \frac{15 \sin (f x + e)}{8} \right) \cos (f x + e)}{6} + \frac{5 f x}{16} + \frac{5 e}{16} \right) - \frac{\sin (f x + e)^6}{36} \right)$$

$$- 4 c f \left( - \frac{\cos (f x + e)^3 \sin (f x + e)^3}{6} - \frac{\cos (f x + e)^3 \sin (f x + e)}{8} + \frac{\cos (f x + e) \sin (f x + e)}{16} + \frac{f x}{16} + \frac{e}{16} \right) + 4 d e \left( - \frac{\cos (f x + e)^3 \sin (f x + e)^3}{6} \right.$$

$$\left. - \frac{\cos (f x + e)^3 \sin (f x + e)}{8} + \frac{\cos (f x + e) \sin (f x + e)}{16} + \frac{f x}{16} + \frac{e}{16} \right) - 3 I d \left( \frac{(f x + e) \sin (f x + e)^4}{4} \right.$$

$$\left. + \frac{\left( \sin (f x + e)^3 + \frac{3 \sin (f x + e)}{2} \right) \cos (f x + e)}{16} - \frac{3 f x}{32} - \frac{3 e}{32} \right) - \frac{3 I c f \sin (f x + e)^4}{4} + \frac{3 I d e \sin (f x + e)^4}{4} + d \left( (f x + e) \left( \right. \right.$$

$$\left. - \frac{\left( \sin (f x + e)^3 + \frac{3 \sin (f x + e)}{2} \right) \cos (f x + e)}{4} + \frac{3 f x}{8} + \frac{3 e}{8} \right) - \frac{3 (f x + e)^2}{16} + \frac{\sin (f x + e)^4}{16} + \frac{3 \sin (f x + e)^2}{16} \right) + c f \left( \right.$$

$$\left. - \frac{\left( \sin (f x + e)^3 + \frac{3 \sin (f x + e)}{2} \right) \cos (f x + e)}{4} + \frac{3 f x}{8} + \frac{3 e}{8} \right) - d e \left( - \frac{\left( \sin (f x + e)^3 + \frac{3 \sin (f x + e)}{2} \right) \cos (f x + e)}{4} + \frac{3 f x}{8} + \frac{3 e}{8} \right)$$

Problem 12: Unable to integrate problem.

$$\int \frac{(d x + c)^m}{(a + I a \cot (f x + e))^2} d x$$

Optimal (type 4, 159 leaves, 4 steps):



$$\frac{(dx+c)^{1+m}}{4a^2d(1+m)} + \frac{12^{-2-m}e^{2I\left(e-\frac{cf}{d}\right)}(dx+c)^m\Gamma\left(1+m,\frac{-2If(dx+c)}{d}\right)}{a^2f\left(\frac{-If(dx+c)}{d}\right)^m} - \frac{14^{-2-m}e^{4I\left(e-\frac{cf}{d}\right)}(dx+c)^m\Gamma\left(1+m,\frac{-4If(dx+c)}{d}\right)}{a^2f\left(\frac{-If(dx+c)}{d}\right)^m}$$

Result(type 8, 24 leaves):

$$\int \frac{(dx+c)^m}{(a+Ia\cot(fx+e))^2} dx$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int (dx+c)(a+b\cot(fx+e)) dx$$

Optimal(type 4, 71 leaves, 6 steps):

$$\frac{a(dx+c)^2}{2d} - \frac{Ib(dx+c)^2}{2d} + \frac{b(dx+c)\ln(1-e^{2I(fx+e)})}{f} - \frac{Ibd\text{polylog}(2, e^{2I(fx+e)})}{2f^2}$$

Result(type 4, 239 leaves):

$$\begin{aligned} & -\frac{Ibd\text{polylog}(2, -e^{I(fx+e)})}{f^2} - \frac{Ibdx^2}{2} + \frac{adx^2}{2} + acx - \frac{2bcln(e^{I(fx+e)})}{f} + \frac{bcln(e^{I(fx+e)}+1)}{f} + \frac{bcln(e^{I(fx+e)}-1)}{f} + Ibcx \\ & - \frac{Ibd\text{polylog}(2, e^{I(fx+e)})}{f^2} - \frac{2Ibdex}{f} + \frac{bdln(1-e^{I(fx+e)})x}{f} + \frac{bdln(1-e^{I(fx+e)})e}{f^2} - \frac{Ibde^2}{f^2} + \frac{bdln(e^{I(fx+e)}+1)x}{f} + \frac{2bdeln(e^{I(fx+e)})}{f^2} \\ & - \frac{bdeln(e^{I(fx+e)}-1)}{f^2} \end{aligned}$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int (dx+c)^3(a+b\cot(fx+e))^3 dx$$

Optimal(type 4, 535 leaves, 28 steps):

$$\begin{aligned} & \frac{3Ib^3d(dx+c)^2\text{polylog}(2, e^{2I(fx+e)})}{2f^2} + \frac{Ib^3(dx+c)^4}{4d} - \frac{b^3(dx+c)^3}{2f} + \frac{a^3(dx+c)^4}{4d} - \frac{3Ib^3d^3\text{polylog}(2, e^{2I(fx+e)})}{2f^4} - \frac{3ab^2(dx+c)^4}{4d} \\ & - \frac{3Ib^3d^3\text{polylog}(4, e^{2I(fx+e)})}{4f^4} - \frac{3b^3d(dx+c)^2\cot(fx+e)}{2f^2} - \frac{3ab^2(dx+c)^3\cot(fx+e)}{f} - \frac{b^3(dx+c)^3\cot(fx+e)^2}{2f} \\ & + \frac{3b^3d^2(dx+c)\ln(1-e^{2I(fx+e)})}{f^3} + \frac{9a^2bd(dx+c)^2\ln(1-e^{2I(fx+e)})}{f^2} + \frac{3a^2b(dx+c)^3\ln(1-e^{2I(fx+e)})}{f} - \frac{b^3(dx+c)^3\ln(1-e^{2I(fx+e)})}{f} \\ & - \frac{9Ia^2bd(dx+c)^2\text{polylog}(2, e^{2I(fx+e)})}{2f^2} - \frac{3Ia^2b(dx+c)^4}{4d} - \frac{9Iab^2d^2(dx+c)\text{polylog}(2, e^{2I(fx+e)})}{f^3} - \frac{3Iab^2(dx+c)^3}{f} \\ & + \frac{9a^2bd^3\text{polylog}(3, e^{2I(fx+e)})}{2f^4} + \frac{9a^2bd^2(dx+c)\text{polylog}(3, e^{2I(fx+e)})}{2f^3} - \frac{3b^3d^2(dx+c)\text{polylog}(3, e^{2I(fx+e)})}{2f^3} \end{aligned}$$

$$+ \frac{9Ia^2 b d^3 \text{polylog}(4, e^{2I(fx+e)})}{4f^4} - \frac{3Ib^3 d (dx+c)^2}{2f^2}$$

Result(type ?, 3112 leaves): Display of huge result suppressed!

Problem 17: Result more than twice size of optimal antiderivative.

$$\int (dx+c) (a+b \cot(fx+e))^3 dx$$

Optimal(type 4, 248 leaves, 16 steps):

$$\begin{aligned} & -3ab^2 cx - \frac{b^3 dx}{2f} - \frac{3ab^2 dx^2}{2} + \frac{a^3 (dx+c)^2}{2d} - \frac{3Ia^2 b (dx+c)^2}{2d} + \frac{Ib^3 (dx+c)^2}{2d} - \frac{b^3 d \cot(fx+e)}{2f^2} - \frac{3ab^2 (dx+c) \cot(fx+e)}{f} \\ & - \frac{b^3 (dx+c) \cot(fx+e)^2}{2f} + \frac{3a^2 b (dx+c) \ln(1-e^{2I(fx+e)})}{f} - \frac{b^3 (dx+c) \ln(1-e^{2I(fx+e)})}{f} + \frac{3ab^2 d \ln(\sin(fx+e))}{f^2} \\ & - \frac{3Ia^2 b d \text{polylog}(2, e^{2I(fx+e)})}{2f^2} + \frac{Ib^3 d \text{polylog}(2, e^{2I(fx+e)})}{2f^2} \end{aligned}$$

Result(type 4, 744 leaves):

$$\begin{aligned} & -3ab^2 cx - \frac{3ab^2 dx^2}{2} + \frac{3b^2 ad \ln(e^{I(fx+e)} - 1)}{f^2} - \frac{6ba^2 c \ln(e^{I(fx+e)})}{f} + \frac{3ba^2 c \ln(e^{I(fx+e)} + 1)}{f} + \frac{3ba^2 c \ln(e^{I(fx+e)} - 1)}{f} \\ & + \frac{Ib^3 d \text{polylog}(2, e^{I(fx+e)})}{f^2} + \frac{Ib^3 d \text{polylog}(2, -e^{I(fx+e)})}{f^2} - \frac{2b^3 de \ln(e^{I(fx+e)})}{f^2} + \frac{b^3 de \ln(e^{I(fx+e)} - 1)}{f^2} + \frac{Ib^3 d e^2}{f^2} - \frac{6b^2 ad \ln(e^{I(fx+e)})}{f^2} \\ & + \frac{3b^2 ad \ln(e^{I(fx+e)} + 1)}{f^2} - \frac{b^3 \ln(1 - e^{I(fx+e)}) de}{f^2} - \frac{b^3 \ln(e^{I(fx+e)} + 1) dx}{f} - \frac{b^3 \ln(1 - e^{I(fx+e)}) dx}{f} - \frac{3Ia^2 b dx^2}{2} - Icb^3 x + a^3 cx + \frac{a^3 dx^2}{2} \\ & - \frac{6Iba^2 dex}{f} + \frac{2b^3 c \ln(e^{I(fx+e)})}{f} - \frac{b^3 c \ln(e^{I(fx+e)} + 1)}{f} - \frac{b^3 c \ln(e^{I(fx+e)} - 1)}{f} + \frac{Ib^3 dx^2}{2} \\ & + \frac{b^2 (-6Iadfx e^{2I(fx+e)} - 6Iacfe^{2I(fx+e)} + 2bdfxe^{2I(fx+e)} + 6Iadfx - Ibde^{2I(fx+e)} + 2bcfe^{2I(fx+e)} + 6Iacf + Ibd)}{f^2 (e^{2I(fx+e)} - 1)^2} \\ & + \frac{6ba^2 de \ln(e^{I(fx+e)})}{f^2} - \frac{3ba^2 de \ln(e^{I(fx+e)} - 1)}{f^2} - \frac{3Iba^2 d \text{polylog}(2, e^{I(fx+e)})}{f^2} - \frac{3Iba^2 d \text{polylog}(2, -e^{I(fx+e)})}{f^2} - \frac{3Iba^2 d e^2}{f^2} + \frac{2Ib^3 dex}{f} \\ & + \frac{3b \ln(1 - e^{I(fx+e)}) a^2 de}{f^2} + \frac{3b \ln(1 - e^{I(fx+e)}) a^2 dx}{f} + \frac{3b \ln(e^{I(fx+e)} + 1) a^2 dx}{f} + 3Icba^2 x \end{aligned}$$

Problem 19: Result more than twice size of optimal antiderivative.

$$\int \frac{dx+c}{(a+b \cot(fx+e))^2} dx$$

Optimal(type 4, 198 leaves, 5 steps):

$$-\frac{(dx+c)^2}{2(a^2+b^2)d} + \frac{(-2adfx-2acf+bd)^2}{4a(a-1b)^2(1b+a)df^2} + \frac{b(dx+c)}{(a^2+b^2)f(a+b\cot(fx+e))} + \frac{b(-2adfx-2acf+bd)\ln\left(1-\frac{(1b+a)e^{21(fx+e)}}{a-1b}\right)}{(a^2+b^2)^2f^2}$$

$$+ \frac{1abd\operatorname{polylog}\left(2, \frac{(1b+a)e^{21(fx+e)}}{a-1b}\right)}{(a^2+b^2)^2f^2}$$

Result(type 4, 989 leaves):

$$\frac{dx^2}{2(2Iab+a^2-b^2)} + \frac{cx}{2Iab+a^2-b^2} + \frac{2Ib^2(dx+c)}{(b+Ia)f(b-Ia)^2(be^{21(fx+e)}-Iae^{21(fx+e)}+b+Ia)}$$

$$- \frac{2Iba^2c\ln(ae^{21(fx+e)}+Ibe^{21(fx+e)}-a+Ib)}{(b+Ia)f(b-Ia)^2(1b-a)(1b+a)} + \frac{2Ibad\ln\left(1-\frac{(1b+a)e^{21(fx+e)}}{a-1b}\right)e}{(b+Ia)f^2(b-Ia)^2(a-1b)} - \frac{b^3d\ln(ae^{21(fx+e)}+Ibe^{21(fx+e)}-a+Ib)}{(b+Ia)f^2(b-Ia)^2(1b-a)(1b+a)}$$

$$+ \frac{Ib^2d\ln(ae^{21(fx+e)}+Ibe^{21(fx+e)}-a+Ib)a}{(b+Ia)f^2(b-Ia)^2(1b-a)(1b+a)} + \frac{2Iba^2de\ln(ae^{21(fx+e)}+Ibe^{21(fx+e)}-a+Ib)}{(b+Ia)f^2(b-Ia)^2(1b-a)(1b+a)}$$

$$+ \frac{2b^2ac\ln(ae^{21(fx+e)}+Ibe^{21(fx+e)}-a+Ib)}{(b+Ia)f(b-Ia)^2(1b-a)(1b+a)} - \frac{2Ib^2d\ln(e^{1(fx+e)})}{(b+Ia)f^2(b-Ia)^2(1b-a)} + \frac{4Ibac\ln(e^{1(fx+e)})}{(b+Ia)f(b-Ia)^2(1b-a)}$$

$$- \frac{2b^2ade\ln(ae^{21(fx+e)}+Ibe^{21(fx+e)}-a+Ib)}{(b+Ia)f^2(b-Ia)^2(1b-a)(1b+a)} + \frac{2Ibad\ln\left(1-\frac{(1b+a)e^{21(fx+e)}}{a-1b}\right)x}{(b+Ia)f(b-Ia)^2(a-1b)} - \frac{4Ibade\ln(e^{1(fx+e)})}{(b+Ia)f^2(b-Ia)^2(1b-a)}$$

$$+ \frac{2badx^2}{(b+Ia)(b-Ia)^2(a-1b)} + \frac{4badex}{(b+Ia)f(b-Ia)^2(a-1b)} + \frac{2bade^2}{(b+Ia)f^2(b-Ia)^2(a-1b)} + \frac{bad\operatorname{polylog}\left(2, \frac{(1b+a)e^{21(fx+e)}}{a-1b}\right)}{(b+Ia)f^2(b-Ia)^2(a-1b)}$$

Test results for the 30 problems in "4.4.2.1 (a+b cot)^m (c+d cot)^n.txt"

Problem 1: Unable to integrate problem.

$$\int (a+Ia\cot(dx+c))^n dx$$

Optimal(type 5, 42 leaves, 2 steps):

$$\frac{\frac{1}{2}(a+Ia\cot(dx+c))^n \operatorname{hypergeom}\left([1, n], [1+n], \frac{1}{2} + \frac{I\cot(dx+c)}{2}\right)}{dn}$$

Result(type 8, 16 leaves):

$$\int (a+Ia\cot(dx+c))^n dx$$

Problem 2: Result more than twice size of optimal antiderivative.

$$\int (e \cot(dx+c))^{3/2} (a + a \cot(dx+c)) dx$$

Optimal(type 3, 77 leaves, 4 steps):

$$-\frac{2a(e \cot(dx+c))^{3/2}}{3d} - \frac{ae^{3/2} \arctan\left(\frac{(\sqrt{e} - \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e \cot(dx+c)}}\right)\sqrt{2}}{d} - \frac{2ae\sqrt{e \cot(dx+c)}}{d}$$

Result(type 3, 362 leaves):

$$\begin{aligned} & -\frac{2a(e \cot(dx+c))^{3/2}}{3d} - \frac{2ae\sqrt{e \cot(dx+c)}}{d} + \frac{ae(e^2)^{1/4}\sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{4d} \\ & + \frac{ae(e^2)^{1/4}\sqrt{2} \arctan\left(\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2d} - \frac{ae(e^2)^{1/4}\sqrt{2} \arctan\left(-\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2d} \\ & + \frac{ae^2\sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{4d(e^2)^{1/4}} + \frac{ae^2\sqrt{2} \arctan\left(\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2d(e^2)^{1/4}} \\ & - \frac{ae^2\sqrt{2} \arctan\left(-\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2d(e^2)^{1/4}} \end{aligned}$$

Problem 3: Result more than twice size of optimal antiderivative.

$$\int \frac{a + a \cot(dx+c)}{(e \cot(dx+c))^{5/2}} dx$$

Optimal(type 3, 82 leaves, 4 steps):

$$\frac{2a}{3de(e \cot(dx+c))^{3/2}} - \frac{a \arctan\left(\frac{(\sqrt{e} - \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e \cot(dx+c)}}\right)\sqrt{2}}{de^{5/2}} + \frac{2a}{de^2\sqrt{e \cot(dx+c)}}$$

Result(type 3, 373 leaves):

$$\frac{2a}{de^2\sqrt{e \cot(dx+c)}} + \frac{2a}{3de(e \cot(dx+c))^{3/2}} + \frac{ae^2(e^2)^{1/4}\sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{4de^3}$$

$$\begin{aligned}
& + \frac{a (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e^3} - \frac{a (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e^3} \\
& + \frac{a \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{4 d e^2 (e^2)^{1/4}} + \frac{a \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e^2 (e^2)^{1/4}} \\
& - \frac{a \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e^2 (e^2)^{1/4}}
\end{aligned}$$

Problem 5: Result more than twice size of optimal antiderivative.

$$\int (e \cot(dx+c))^5 / 2 (a + a \cot(dx+c))^3 dx$$

Optimal (type 3, 157 leaves, 7 steps):

$$\begin{aligned}
& \frac{4 a^3 e (e \cot(dx+c))^3 / 2}{3 d} - \frac{4 a^3 (e \cot(dx+c))^5 / 2}{5 d} - \frac{40 a^3 (e \cot(dx+c))^7 / 2}{63 d e} - \frac{2 (e \cot(dx+c))^7 / 2 (a^3 + a^3 \cot(dx+c))}{9 d e} \\
& + \frac{2 a^3 e^5 / 2 \arctan\left(\frac{(\sqrt{e} - \cot(dx+c) \sqrt{e}) \sqrt{2}}{2 \sqrt{e \cot(dx+c)}}\right) \sqrt{2}}{d} + \frac{4 a^3 e^2 \sqrt{e \cot(dx+c)}}{d}
\end{aligned}$$

Result (type 3, 445 leaves):

$$\begin{aligned}
& - \frac{2 a^3 (e \cot(dx+c))^9 / 2}{9 d e^2} - \frac{6 a^3 (e \cot(dx+c))^7 / 2}{7 d e} - \frac{4 a^3 (e \cot(dx+c))^5 / 2}{5 d} + \frac{4 a^3 e (e \cot(dx+c))^3 / 2}{3 d} + \frac{4 a^3 e^2 \sqrt{e \cot(dx+c)}}{d} \\
& - \frac{a^3 e^2 (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2 d} - \frac{a^3 e^2 (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d} \\
& + \frac{a^3 e^2 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d} - \frac{a^3 e^3 \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2 d (e^2)^{1/4}} \\
& - \frac{a^3 e^3 \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}} + \frac{a^3 e^3 \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}}
\end{aligned}$$

Problem 6: Result more than twice size of optimal antiderivative.

$$\int (e \cot(dx+c))^3 / 2 (a + a \cot(dx+c))^3 dx$$

Optimal (type 3, 135 leaves, 6 steps):

$$\begin{aligned} & - \frac{4 a^3 (e \cot(dx+c))^3 / 2}{3 d} - \frac{32 a^3 (e \cot(dx+c))^5 / 2}{35 d e} - \frac{2 (e \cot(dx+c))^5 / 2 (a^3 + a^3 \cot(dx+c))}{7 d e} \\ & - \frac{2 a^3 e^3 / 2 \operatorname{arctanh}\left(\frac{(\sqrt{e} + \cot(dx+c) \sqrt{e}) \sqrt{2}}{2 \sqrt{e \cot(dx+c)}}\right) \sqrt{2}}{d} + \frac{4 a^3 e \sqrt{e \cot(dx+c)}}{d} \end{aligned}$$

Result (type 3, 418 leaves):

$$\begin{aligned} & - \frac{2 a^3 (e \cot(dx+c))^7 / 2}{7 d e^2} - \frac{6 a^3 (e \cot(dx+c))^5 / 2}{5 d e} - \frac{4 a^3 (e \cot(dx+c))^3 / 2}{3 d} + \frac{4 a^3 e \sqrt{e \cot(dx+c)}}{d} \\ & - \frac{a^3 e (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2 d} - \frac{a^3 e (e^2)^{1/4} \sqrt{2} \operatorname{arctan}\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d} \\ & + \frac{a^3 e (e^2)^{1/4} \sqrt{2} \operatorname{arctan}\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d} + \frac{a^3 e^2 \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2 d (e^2)^{1/4}} \\ & + \frac{a^3 e^2 \sqrt{2} \operatorname{arctan}\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}} - \frac{a^3 e^2 \sqrt{2} \operatorname{arctan}\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}} \end{aligned}$$

Problem 7: Result more than twice size of optimal antiderivative.

$$\int \sqrt{e \cot(dx+c)} (a + a \cot(dx+c))^3 dx$$

Optimal (type 3, 117 leaves, 5 steps):

$$\begin{aligned} & - \frac{8 a^3 (e \cot(dx+c))^3 / 2}{5 d e} - \frac{2 (e \cot(dx+c))^3 / 2 (a^3 + a^3 \cot(dx+c))}{5 d e} - \frac{2 a^3 \operatorname{arctan}\left(\frac{(\sqrt{e} - \cot(dx+c) \sqrt{e}) \sqrt{2}}{2 \sqrt{e \cot(dx+c)}}\right) \sqrt{2} \sqrt{e}}{d} - \frac{4 a^3 \sqrt{e \cot(dx+c)}}{d} \end{aligned}$$

Result (type 3, 390 leaves):

$$\begin{aligned} & - \frac{2 a^3 (e \cot(dx+c))^5 / 2}{5 d e^2} - \frac{2 a^3 (e \cot(dx+c))^3 / 2}{d e} - \frac{4 a^3 \sqrt{e \cot(dx+c)}}{d} \\ & + \frac{a^3 (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2 d} + \frac{a^3 (e^2)^{1/4} \sqrt{2} \operatorname{arctan}\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d} \end{aligned}$$

$$\begin{aligned}
& - \frac{a^3 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d} + \frac{a^3 e \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2d (e^2)^{1/4}} \\
& + \frac{a^3 e \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}} - \frac{a^3 e \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}}
\end{aligned}$$

Problem 8: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \cot(dx+c))^3}{\sqrt{e \cot(dx+c)}} dx$$

Optimal(type 3, 98 leaves, 4 steps):

$$\frac{2a^3 \operatorname{arctanh}\left(\frac{(\sqrt{e} + \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e \cot(dx+c)}}\right)\sqrt{2}}{d\sqrt{e}} - \frac{16a^3 \sqrt{e \cot(dx+c)}}{3de} - \frac{2(a^3 + a^3 \cot(dx+c))\sqrt{e \cot(dx+c)}}{3de}$$

Result(type 3, 378 leaves):

$$\begin{aligned}
& - \frac{2a^3 (e \cot(dx+c))^3 / 2}{3de^2} - \frac{6a^3 \sqrt{e \cot(dx+c)}}{de} + \frac{a^3 (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2de} \\
& + \frac{a^3 (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{de} - \frac{a^3 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{de} \\
& - \frac{a^3 \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2d (e^2)^{1/4}} - \frac{a^3 \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}} \\
& + \frac{a^3 \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}}
\end{aligned}$$

Problem 9: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \cot(dx+c))^3}{(e \cot(dx+c))^{3/2}} dx$$

Optimal(type 3, 99 leaves, 4 steps):

$$\frac{2a^3 \arctan\left(\frac{(\sqrt{e} - \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e\cot(dx+c)}}\right)\sqrt{2}}{de^3/2} + \frac{2(a^3 + a^3 \cot(dx+c))}{de\sqrt{e\cot(dx+c)}} - \frac{4a^3\sqrt{e\cot(dx+c)}}{de^2}$$

Result(type 3, 387 leaves):

$$\begin{aligned} & -\frac{2a^3\sqrt{e\cot(dx+c)}}{de^2} - \frac{a^3(e^2)^{1/4}\sqrt{2}\ln\left(\frac{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{2de^2} - \frac{a^3(e^2)^{1/4}\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{de^2} \\ & + \frac{a^3(e^2)^{1/4}\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{de^2} - \frac{a^3\sqrt{2}\ln\left(\frac{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{2de(e^2)^{1/4}} \\ & - \frac{a^3\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{de(e^2)^{1/4}} + \frac{a^3\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{de(e^2)^{1/4}} + \frac{2a^3}{de\sqrt{e\cot(dx+c)}} \end{aligned}$$

Problem 10: Result more than twice size of optimal antiderivative.

$$\int \frac{(e\cot(dx+c))^5/2}{a+a\cot(dx+c)} dx$$

Optimal(type 3, 92 leaves, 7 steps):

$$\frac{e^5/2 \arctan\left(\frac{\sqrt{e\cot(dx+c)}}{\sqrt{e}}\right)}{ad} - \frac{e^5/2 \arctan\left(\frac{(\sqrt{e} - \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e\cot(dx+c)}}\right)\sqrt{2}}{2ad} - \frac{2e^2\sqrt{e\cot(dx+c)}}{ad}$$

Result(type 3, 393 leaves):

$$\begin{aligned} & -\frac{2e^2\sqrt{e\cot(dx+c)}}{ad} + \frac{e^5/2 \arctan\left(\frac{\sqrt{e\cot(dx+c)}}{\sqrt{e}}\right)}{ad} + \frac{e^2(e^2)^{1/4}\sqrt{2}\ln\left(\frac{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{8da} \\ & + \frac{e^2(e^2)^{1/4}\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{4da} - \frac{e^2(e^2)^{1/4}\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{4da} \\ & + \frac{e^3\sqrt{2}\ln\left(\frac{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{8da(e^2)^{1/4}} + \frac{e^3\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{4da(e^2)^{1/4}} \end{aligned}$$



$$-\frac{e^3 \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{4da(e^2)^{1/4}}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cot(dx+c))^{5/2}}{(a+a \cot(dx+c))^3} dx$$

Optimal (type 3, 135 leaves, 8 steps):

$$-\frac{e^5/2 \arctan\left(\frac{\sqrt{e \cot(dx+c)}}{\sqrt{e}}\right)}{8a^3d} + \frac{e^5/2 \operatorname{arctanh}\left(\frac{(\sqrt{e} + \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e \cot(dx+c)}}\right)\sqrt{2}}{4a^3d} - \frac{5e^2\sqrt{e \cot(dx+c)}}{8a^3d(1+\cot(dx+c))} + \frac{e^2\sqrt{e \cot(dx+c)}}{4ad(a+a \cot(dx+c))^2}$$

Result (type 3, 439 leaves):

$$\begin{aligned} &-\frac{5e^3(e \cot(dx+c))^3/2}{8da^3(e \cot(dx+c)+e)^2} - \frac{3e^4\sqrt{e \cot(dx+c)}}{8da^3(e \cot(dx+c)+e)^2} - \frac{e^5/2 \arctan\left(\frac{\sqrt{e \cot(dx+c)}}{\sqrt{e}}\right)}{8a^3d} \\ &+ \frac{e^2(e^2)^{1/4}\sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{16da^3} + \frac{e^2(e^2)^{1/4}\sqrt{2} \arctan\left(\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{8da^3} \\ &- \frac{e^2(e^2)^{1/4}\sqrt{2} \arctan\left(-\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{8da^3} - \frac{e^3\sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4}\sqrt{e \cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)}{16da^3(e^2)^{1/4}} \\ &- \frac{e^3\sqrt{2} \arctan\left(\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{8da^3(e^2)^{1/4}} + \frac{e^3\sqrt{2} \arctan\left(-\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{8da^3(e^2)^{1/4}} \end{aligned}$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cot(dx+c))^{3/2}(a+a \cot(dx+c))^3} dx$$

Optimal (type 3, 156 leaves, 9 steps):

$$\frac{31 \arctan\left(\frac{\sqrt{e \cot(dx+c)}}{\sqrt{e}}\right)}{8a^3de^3/2} + \frac{\operatorname{arctanh}\left(\frac{(\sqrt{e} + \cot(dx+c)\sqrt{e})\sqrt{2}}{2\sqrt{e \cot(dx+c)}}\right)\sqrt{2}}{4a^3de^3/2} + \frac{27}{8a^3de\sqrt{e \cot(dx+c)}} - \frac{9}{8a^3de(1+\cot(dx+c))\sqrt{e \cot(dx+c)}}$$

$$-\frac{1}{4ade(a+a\cot(dx+c))^2\sqrt{e\cot(dx+c)}}$$

Result(type 3, 457 leaves):

$$\begin{aligned} & \frac{11(e\cot(dx+c))^3/2}{8da^3e(e\cot(dx+c)+e)^2} + \frac{13\sqrt{e\cot(dx+c)}}{8da^3(e\cot(dx+c)+e)^2} + \frac{31\arctan\left(\frac{\sqrt{e\cot(dx+c)}}{\sqrt{e}}\right)}{8a^3de^3/2} + \frac{2}{a^3de\sqrt{e\cot(dx+c)}} \\ & + \frac{(e^2)^{1/4}\sqrt{2}\ln\left(\frac{e\cot(dx+c)+(e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2}+\sqrt{e^2}}{e\cot(dx+c)-(e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2}+\sqrt{e^2}}\right)}{16da^3e^2} + \frac{(e^2)^{1/4}\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}}+1\right)}{8da^3e^2} \\ & - \frac{(e^2)^{1/4}\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}}+1\right)}{8da^3e^2} - \frac{\sqrt{2}\ln\left(\frac{e\cot(dx+c)-(e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2}+\sqrt{e^2}}{e\cot(dx+c)+(e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2}+\sqrt{e^2}}\right)}{16da^3e(e^2)^{1/4}} \\ & - \frac{\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}}+1\right)}{8da^3e(e^2)^{1/4}} + \frac{\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}}+1\right)}{8da^3e(e^2)^{1/4}} \end{aligned}$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \cot(x)^2 \sqrt{1+\cot(x)} dx$$

Optimal(type 3, 160 leaves, 12 steps):

$$\begin{aligned} & -\frac{2(1+\cot(x))^3/2}{3} - \frac{\arctan\left(\frac{-2\sqrt{1+\cot(x)}+\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)\sqrt{2+2\sqrt{2}}}{2} + \frac{\arctan\left(\frac{2\sqrt{1+\cot(x)}+\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)\sqrt{2+2\sqrt{2}}}{2} \\ & + \frac{\ln\left(1+\cot(x)+\sqrt{2}-\sqrt{1+\cot(x)}\sqrt{2+2\sqrt{2}}\right)}{2\sqrt{2+2\sqrt{2}}} - \frac{\ln\left(1+\cot(x)+\sqrt{2}+\sqrt{1+\cot(x)}\sqrt{2+2\sqrt{2}}\right)}{2\sqrt{2+2\sqrt{2}}} \end{aligned}$$

Result(type 3, 355 leaves):

$$-\frac{2(1+\cot(x))^3/2}{3} + \frac{\sqrt{2+2\sqrt{2}}\sqrt{2}\ln\left(1+\cot(x)+\sqrt{2}-\sqrt{1+\cot(x)}\sqrt{2+2\sqrt{2}}\right)}{4} + \frac{\sqrt{2}(2+2\sqrt{2})\arctan\left(\frac{2\sqrt{1+\cot(x)}-\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}}$$

$$\begin{aligned}
& - \frac{\sqrt{2+2\sqrt{2}} \ln\left(1 + \cot(x) + \sqrt{2} - \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4} - \frac{(2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} - \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} \\
& - \frac{\sqrt{2+2\sqrt{2}} \sqrt{2} \ln\left(1 + \cot(x) + \sqrt{2} + \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4} + \frac{\sqrt{2} (2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} \\
& + \frac{\sqrt{2+2\sqrt{2}} \ln\left(1 + \cot(x) + \sqrt{2} + \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4} - \frac{(2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}}
\end{aligned}$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot(x)^2}{\sqrt{1 + \cot(x)}} dx$$

Optimal (type 3, 152 leaves, 12 steps):

$$\begin{aligned}
& -2\sqrt{1 + \cot(x)} - \frac{\ln\left(1 + \cot(x) + \sqrt{2} - \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4\sqrt{1 + \sqrt{2}}} + \frac{\ln\left(1 + \cot(x) + \sqrt{2} + \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4\sqrt{1 + \sqrt{2}}} \\
& - \frac{\arctan\left(\frac{-2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right) \sqrt{1 + \sqrt{2}}}{2} + \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right) \sqrt{1 + \sqrt{2}}}{2}
\end{aligned}$$

Result (type 3, 441 leaves):

$$\begin{aligned}
& -2\sqrt{1 + \cot(x)} - \frac{\sqrt{2+2\sqrt{2}} \ln\left(1 + \cot(x) + \sqrt{2} - \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4} + \frac{\sqrt{2+2\sqrt{2}} \sqrt{2} \ln\left(1 + \cot(x) + \sqrt{2} - \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{8} \\
& + \frac{\sqrt{2} (2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} - \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{4\sqrt{-2+2\sqrt{2}}} - \frac{(2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} - \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} \\
& + \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} - \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right) \sqrt{2}}{\sqrt{-2+2\sqrt{2}}} + \frac{\sqrt{2+2\sqrt{2}} \ln\left(1 + \cot(x) + \sqrt{2} + \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{4}
\end{aligned}$$

$$\begin{aligned}
& - \frac{\sqrt{2+2\sqrt{2}} \sqrt{2} \ln\left(1 + \cot(x) + \sqrt{2} + \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{8} + \frac{\sqrt{2} (2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{4\sqrt{-2+2\sqrt{2}}} \\
& - \frac{(2+2\sqrt{2}) \arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} + \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right) \sqrt{2}}{\sqrt{-2+2\sqrt{2}}}
\end{aligned}$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot(x)^2}{(1 + \cot(x))^3} \frac{1}{2} dx$$

Optimal (type 3, 97 leaves, 6 steps):

$$\frac{1}{\sqrt{1 + \cot(x)}} + \frac{\arctan\left(\frac{4 + \cot(x)(2 - \sqrt{2}) - 3\sqrt{2}}{2\sqrt{1 + \cot(x)} \sqrt{-7 + 5\sqrt{2}}}\right) \sqrt{-2 + 2\sqrt{2}}}{4} + \frac{\operatorname{arctanh}\left(\frac{4 + 3\sqrt{2} + \cot(x)(2 + \sqrt{2})}{2\sqrt{1 + \cot(x)} \sqrt{7 + 5\sqrt{2}}}\right) \sqrt{2 + 2\sqrt{2}}}{4}$$

Result (type 3, 248 leaves):

$$\begin{aligned}
& - \frac{\sqrt{2+2\sqrt{2}} \ln\left(1 + \cot(x) + \sqrt{2} - \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{8} + \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} - \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right) \sqrt{2}}{2\sqrt{-2+2\sqrt{2}}} \\
& - \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} - \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} + \frac{\sqrt{2+2\sqrt{2}} \ln\left(1 + \cot(x) + \sqrt{2} + \sqrt{1 + \cot(x)} \sqrt{2+2\sqrt{2}}\right)}{8} \\
& + \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right) \sqrt{2}}{2\sqrt{-2+2\sqrt{2}}} - \frac{\arctan\left(\frac{2\sqrt{1 + \cot(x)} + \sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} + \frac{1}{\sqrt{1 + \cot(x)}}
\end{aligned}$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot(x)^2}{(1 + \cot(x))^5} \frac{1}{2} dx$$

Optimal(type 3, 101 leaves, 8 steps):

$$\frac{1}{3(1+\cot(x))^3/2} - \frac{1}{\sqrt{1+\cot(x)}} + \frac{\arctan\left(\frac{3+\cot(x)(1-\sqrt{2})-2\sqrt{2}}{\sqrt{1+\cot(x)}\sqrt{-14+10\sqrt{2}}}\right)\sqrt{\sqrt{2}-1}}{4} + \frac{\operatorname{arctanh}\left(\frac{3+2\sqrt{2}+\cot(x)(1+\sqrt{2})}{\sqrt{1+\cot(x)}\sqrt{14+10\sqrt{2}}}\right)\sqrt{1+\sqrt{2}}}{4}$$

Result(type 3, 264 leaves):

$$\begin{aligned} & \frac{1}{3(1+\cot(x))^3/2} - \frac{1}{\sqrt{1+\cot(x)}} - \frac{\sqrt{2+2\sqrt{2}}\sqrt{2}\ln\left(1+\cot(x)+\sqrt{2}-\sqrt{1+\cot(x)}\sqrt{2+2\sqrt{2}}\right)}{16} - \frac{\arctan\left(\frac{2\sqrt{1+\cot(x)}-\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} \\ & + \frac{\arctan\left(\frac{2\sqrt{1+\cot(x)}-\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)\sqrt{2}}{4\sqrt{-2+2\sqrt{2}}} + \frac{\sqrt{2+2\sqrt{2}}\sqrt{2}\ln\left(1+\cot(x)+\sqrt{2}+\sqrt{1+\cot(x)}\sqrt{2+2\sqrt{2}}\right)}{16} \\ & - \frac{\arctan\left(\frac{2\sqrt{1+\cot(x)}+\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)}{2\sqrt{-2+2\sqrt{2}}} + \frac{\arctan\left(\frac{2\sqrt{1+\cot(x)}+\sqrt{2+2\sqrt{2}}}{\sqrt{-2+2\sqrt{2}}}\right)\sqrt{2}}{4\sqrt{-2+2\sqrt{2}}} \end{aligned}$$

Problem 18: Result more than twice size of optimal antiderivative.

$$\int (e \cot(dx+c))^3/2 (a+b \cot(dx+c))^2 dx$$

Optimal(type 3, 260 leaves, 13 steps):

$$\begin{aligned} & -\frac{4ab(e \cot(dx+c))^3/2}{3d} - \frac{2b^2(e \cot(dx+c))^5/2}{5de} - \frac{(a^2+2ab-b^2)e^3/2 \arctan\left(1-\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{\sqrt{e}}\right)\sqrt{2}}{2d} \\ & + \frac{(a^2+2ab-b^2)e^3/2 \arctan\left(1+\frac{\sqrt{2}\sqrt{e \cot(dx+c)}}{\sqrt{e}}\right)\sqrt{2}}{2d} - \frac{(a^2-2ab-b^2)e^3/2 \ln\left(\sqrt{e}+\cot(dx+c)\sqrt{e}-\sqrt{2}\sqrt{e \cot(dx+c)}\right)\sqrt{2}}{4d} \\ & + \frac{(a^2-2ab-b^2)e^3/2 \ln\left(\sqrt{e}+\cot(dx+c)\sqrt{e}+\sqrt{2}\sqrt{e \cot(dx+c)}\right)\sqrt{2}}{4d} - \frac{2(a^2-b^2)e\sqrt{e \cot(dx+c)}}{d} \end{aligned}$$

Result(type 3, 580 leaves):

$$-\frac{2b^2(e \cot(dx+c))^5/2}{5de} - \frac{4ab(e \cot(dx+c))^3/2}{3d} - \frac{2ea^2\sqrt{e \cot(dx+c)}}{d} + \frac{2eb^2\sqrt{e \cot(dx+c)}}{d}$$

$$\begin{aligned}
& + \frac{e (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2}{2d} - \frac{e (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^2}{2d} \\
& - \frac{e (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2}{2d} + \frac{e (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^2}{2d} \\
& + \frac{e (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a^2}{4d} \\
& - \frac{e (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) b^2}{4d} \\
& + \frac{e^2 ab \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2d (e^2)^{1/4}} + \frac{e^2 ab \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}} \\
& - \frac{e^2 ab \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d (e^2)^{1/4}}
\end{aligned}$$

Problem 19: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \cot(dx+c))^2}{(e \cot(dx+c))^{3/2}} dx$$

Optimal (type 3, 218 leaves, 11 steps):

$$\begin{aligned}
& - \frac{(a^2 - 2ab - b^2) \arctan\left(1 - \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2d e^{3/2}} + \frac{(a^2 - 2ab - b^2) \arctan\left(1 + \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2d e^{3/2}} \\
& + \frac{(a^2 + 2ab - b^2) \ln\left(\sqrt{e} + \cot(dx+c) \sqrt{e} - \sqrt{2} \sqrt{e \cot(dx+c)}\right) \sqrt{2}}{4d e^{3/2}} \\
& - \frac{(a^2 + 2ab - b^2) \ln\left(\sqrt{e} + \cot(dx+c) \sqrt{e} + \sqrt{2} \sqrt{e \cot(dx+c)}\right) \sqrt{2}}{4d e^{3/2}} + \frac{2a^2}{d e \sqrt{e \cot(dx+c)}}
\end{aligned}$$

Result (type 3, 537 leaves):

$$\begin{aligned}
& - \frac{ab (e^2)^{1/4} \sqrt{2} \ln \left( \frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}} \right)}{2e^2 d} - \frac{ab (e^2)^{1/4} \sqrt{2} \arctan \left( \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right)}{e^2 d} \\
& + \frac{ab (e^2)^{1/4} \sqrt{2} \arctan \left( -\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right)}{e^2 d} + \frac{\sqrt{2} \ln \left( \frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}} \right) a^2}{4ed (e^2)^{1/4}} \\
& - \frac{\sqrt{2} \ln \left( \frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}} \right) b^2}{4ed (e^2)^{1/4}} + \frac{\sqrt{2} \arctan \left( \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) a^2}{2ed (e^2)^{1/4}} \\
& - \frac{\sqrt{2} \arctan \left( \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) b^2}{2ed (e^2)^{1/4}} - \frac{\sqrt{2} \arctan \left( -\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) a^2}{2ed (e^2)^{1/4}} + \frac{\sqrt{2} \arctan \left( -\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) b^2}{2ed (e^2)^{1/4}} \\
& + \frac{2a^2}{de \sqrt{e \cot(dx+c)}}
\end{aligned}$$

Problem 20: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \cot(dx+c))^3}{\sqrt{e \cot(dx+c)}} dx$$

Optimal (type 3, 258 leaves, 12 steps):

$$\begin{aligned}
& \frac{(a-b)(a^2+4ab+b^2) \arctan \left( 1 - \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}} \right) \sqrt{2}}{2d\sqrt{e}} - \frac{(a-b)(a^2+4ab+b^2) \arctan \left( 1 + \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}} \right) \sqrt{2}}{2d\sqrt{e}} \\
& + \frac{(a+b)(a^2-4ab+b^2) \ln(\sqrt{e} + \cot(dx+c) \sqrt{e} - \sqrt{2} \sqrt{e \cot(dx+c)}) \sqrt{2}}{4d\sqrt{e}} \\
& - \frac{(a+b)(a^2-4ab+b^2) \ln(\sqrt{e} + \cot(dx+c) \sqrt{e} + \sqrt{2} \sqrt{e \cot(dx+c)}) \sqrt{2}}{4d\sqrt{e}} - \frac{16ab^2 \sqrt{e \cot(dx+c)}}{3de} \\
& - \frac{2b^2 (a + b \cot(dx+c)) \sqrt{e \cot(dx+c)}}{3de}
\end{aligned}$$

Result (type 3, 724 leaves):

$$\frac{2b^3 (e \cot(dx+c))^3 / 2}{3de^2} - \frac{6ab^2 \sqrt{e \cot(dx+c)}}{de} - \frac{a^3 (e^2)^{1/4} \sqrt{2} \arctan \left( \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right)}{2de}$$

$$\begin{aligned}
& + \frac{3 (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a b^2}{2 d e} + \frac{a^3 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e} \\
& - \frac{3 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a b^2}{2 d e} - \frac{a^3 (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{4 d e} \\
& + \frac{3 (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a b^2}{4 d e} \\
& - \frac{3 \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a^2 b}{4 d (e^2)^{1/4}} + \frac{\sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) b^3}{4 d (e^2)^{1/4}} \\
& - \frac{3 \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2 b}{2 d (e^2)^{1/4}} + \frac{\sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^3}{2 d (e^2)^{1/4}} + \frac{3 \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2 b}{2 d (e^2)^{1/4}} \\
& - \frac{\sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^3}{2 d (e^2)^{1/4}}
\end{aligned}$$

Problem 21: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \cot(dx+c))^3}{(e \cot(dx+c))^{3/2}} dx$$

Optimal (type 3, 262 leaves, 12 steps):

$$\begin{aligned}
& - \frac{(a+b)(a^2 - 4ab + b^2) \arctan\left(1 - \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2 d e^{3/2}} + \frac{(a+b)(a^2 - 4ab + b^2) \arctan\left(1 + \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2 d e^{3/2}} \\
& + \frac{(a-b)(a^2 + 4ab + b^2) \ln\left(\sqrt{e} + \cot(dx+c) \sqrt{e} - \sqrt{2} \sqrt{e \cot(dx+c)}\right) \sqrt{2}}{4 d e^{3/2}} \\
& - \frac{(a-b)(a^2 + 4ab + b^2) \ln\left(\sqrt{e} + \cot(dx+c) \sqrt{e} + \sqrt{2} \sqrt{e \cot(dx+c)}\right) \sqrt{2}}{4 d e^{3/2}} + \frac{2 a^2 (a + b \cot(dx+c))}{d e \sqrt{e \cot(dx+c)}} - \frac{2 b (a^2 + b^2) \sqrt{e \cot(dx+c)}}{d e^2}
\end{aligned}$$

Result (type 3, 741 leaves):



$$\begin{aligned}
& - \frac{2b^3 \sqrt{e \cot(dx+c)}}{d e^2} - \frac{3(e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2 b}{2 d e^2} + \frac{(e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^3}{2 d e^2} \\
& + \frac{3(e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2 b}{2 d e^2} - \frac{(e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^3}{2 d e^2} \\
& - \frac{3(e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a^2 b}{4 d e^2} \\
& + \frac{(e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) b^3}{4 d e^2} + \frac{a^3 \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{4 d e (e^2)^{1/4}} \\
& - \frac{3 \sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a b^2}{4 d e (e^2)^{1/4}} + \frac{a^3 \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e (e^2)^{1/4}} \\
& - \frac{3 \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a b^2}{2 d e (e^2)^{1/4}} - \frac{a^3 \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{2 d e (e^2)^{1/4}} + \frac{3 \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a b^2}{2 d e (e^2)^{1/4}} \\
& + \frac{2a^3}{d e \sqrt{e \cot(dx+c)}}
\end{aligned}$$

Problem 22: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \cot(dx+c))^3}{(e \cot(dx+c))^{5/2}} dx$$

Optimal (type 3, 258 leaves, 12 steps):

$$\begin{aligned}
& \frac{2a^2(a + b \cot(dx+c))}{3 d e (e \cot(dx+c))^{3/2}} - \frac{(a-b)(a^2 + 4ab + b^2) \arctan\left(1 - \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2 d e^{5/2}} \\
& + \frac{(a-b)(a^2 + 4ab + b^2) \arctan\left(1 + \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2 d e^{5/2}}
\end{aligned}$$

$$\begin{aligned}
& - \frac{(a+b)(a^2-4ab+b^2)\ln(\sqrt{e} + \cot(dx+c)\sqrt{e} - \sqrt{2}\sqrt{e\cot(dx+c)})\sqrt{2}}{4de^{5/2}} \\
& + \frac{(a+b)(a^2-4ab+b^2)\ln(\sqrt{e} + \cot(dx+c)\sqrt{e} + \sqrt{2}\sqrt{e\cot(dx+c)})\sqrt{2}}{4de^{5/2}} + \frac{16a^2b}{3de^2\sqrt{e\cot(dx+c)}}
\end{aligned}$$

Result(type 3, 742 leaves):

$$\begin{aligned}
& \frac{2a^3}{3de(e\cot(dx+c))^{3/2}} + \frac{6a^2b}{de^2\sqrt{e\cot(dx+c)}} + \frac{(e^2)^{1/4}\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)a^3}{2de^3} \\
& - \frac{3(e^2)^{1/4}\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)ab^2}{2de^3} - \frac{(e^2)^{1/4}\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)a^3}{2de^3} \\
& + \frac{3(e^2)^{1/4}\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)ab^2}{2de^3} + \frac{(e^2)^{1/4}\sqrt{2}\ln\left(\frac{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)a^3}{4de^3} \\
& - \frac{3(e^2)^{1/4}\sqrt{2}\ln\left(\frac{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)ab^2}{4de^3} \\
& + \frac{3\sqrt{2}\ln\left(\frac{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)a^2b}{4de^2(e^2)^{1/4}} - \frac{\sqrt{2}\ln\left(\frac{e\cot(dx+c) - (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}{e\cot(dx+c) + (e^2)^{1/4}\sqrt{e\cot(dx+c)}\sqrt{2} + \sqrt{e^2}}\right)b^3}{4de^2(e^2)^{1/4}} \\
& + \frac{3\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)a^2b}{2de^2(e^2)^{1/4}} - \frac{\sqrt{2}\arctan\left(\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)b^3}{2de^2(e^2)^{1/4}} - \frac{3\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)a^2b}{2de^2(e^2)^{1/4}} \\
& + \frac{\sqrt{2}\arctan\left(-\frac{\sqrt{2}\sqrt{e\cot(dx+c)}}{(e^2)^{1/4}} + 1\right)b^3}{2de^2(e^2)^{1/4}}
\end{aligned}$$

Problem 24: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(e\cot(dx+c))^{3/2}(a+b\cot(dx+c))^2} dx$$

Optimal(type 3, 372 leaves, 16 steps):

$$\begin{aligned}
& \frac{b^5 / 2 (7a^2 + 3b^2) \arctan\left(\frac{\sqrt{b} \sqrt{e \cot(dx+c)}}{\sqrt{a} \sqrt{e}}\right)}{a^5 / 2 (a^2 + b^2)^2 d e^3 / 2} - \frac{(a^2 + 2ab - b^2) \arctan\left(1 - \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2 (a^2 + b^2)^2 d e^3 / 2} \\
& + \frac{(a^2 + 2ab - b^2) \arctan\left(1 + \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2 (a^2 + b^2)^2 d e^3 / 2} + \frac{(a^2 - 2ab - b^2) \ln(\sqrt{e} + \cot(dx+c) \sqrt{e} - \sqrt{2} \sqrt{e \cot(dx+c)}) \sqrt{2}}{4 (a^2 + b^2)^2 d e^3 / 2} \\
& - \frac{(a^2 - 2ab - b^2) \ln(\sqrt{e} + \cot(dx+c) \sqrt{e} + \sqrt{2} \sqrt{e \cot(dx+c)}) \sqrt{2}}{4 (a^2 + b^2)^2 d e^3 / 2} + \frac{2a^2 + 3b^2}{a^2 (a^2 + b^2) d e \sqrt{e \cot(dx+c)}} \\
& - \frac{b^2}{a (a^2 + b^2) d e (a + b \cot(dx+c)) \sqrt{e \cot(dx+c)}}
\end{aligned}$$

Result(type 3, 802 leaves):

$$\begin{aligned}
& \frac{b^3 \sqrt{e \cot(dx+c)}}{d e (a^2 + b^2)^2 (e \cot(dx+c) b + a e)} + \frac{b^5 \sqrt{e \cot(dx+c)}}{d e a^2 (a^2 + b^2)^2 (e \cot(dx+c) b + a e)} + \frac{7 b^3 \arctan\left(\frac{\sqrt{e \cot(dx+c)} b}{\sqrt{a e b}}\right)}{d e (a^2 + b^2)^2 \sqrt{a e b}} + \frac{3 b^5 \arctan\left(\frac{\sqrt{e \cot(dx+c)} b}{\sqrt{a e b}}\right)}{d e a^2 (a^2 + b^2)^2 \sqrt{a e b}} \\
& + \frac{2}{d e a^2 \sqrt{e \cot(dx+c)}} + \frac{a b (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right)}{2 d e^2 (a^2 + b^2)^2} \\
& + \frac{a b (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d e^2 (a^2 + b^2)^2} - \frac{a b (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right)}{d e^2 (a^2 + b^2)^2} \\
& + \frac{\sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a^2}{4 d e (a^2 + b^2)^2 (e^2)^{1/4}} - \frac{\sqrt{2} \ln\left(\frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) b^2}{4 d e (a^2 + b^2)^2 (e^2)^{1/4}} \\
& + \frac{\sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2}{2 d e (a^2 + b^2)^2 (e^2)^{1/4}} - \frac{\sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^2}{2 d e (a^2 + b^2)^2 (e^2)^{1/4}} - \frac{\sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2}{2 d e (a^2 + b^2)^2 (e^2)^{1/4}} \\
& + \frac{\sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^2}{2 d e (a^2 + b^2)^2 (e^2)^{1/4}}
\end{aligned}$$

Problem 25: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cot(dx+c))^{9/2}}{(a+b \cot(dx+c))^3} dx$$

Optimal (type 3, 454 leaves, 17 steps):

$$\begin{aligned} & \frac{a^5/2 (15a^4 + 46a^2b^2 + 63b^4) e^{9/2} \arctan\left(\frac{\sqrt{b} \sqrt{e \cot(dx+c)}}{\sqrt{a} \sqrt{e}}\right)}{4b^7/2 (a^2+b^2)^3 d} + \frac{a^2 e^2 (e \cot(dx+c))^{5/2}}{2b (a^2+b^2) d (a+b \cot(dx+c))^2} + \frac{a^2 (5a^2+13b^2) e^3 (e \cot(dx+c))^3/2}{4b^2 (a^2+b^2)^2 d (a+b \cot(dx+c))} \\ & + \frac{(a-b) (a^2+4ab+b^2) e^{9/2} \arctan\left(1 - \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2(a^2+b^2)^3 d} - \frac{(a-b) (a^2+4ab+b^2) e^{9/2} \arctan\left(1 + \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{\sqrt{e}}\right) \sqrt{2}}{2(a^2+b^2)^3 d} \\ & - \frac{(a+b) (a^2-4ab+b^2) e^{9/2} \ln(\sqrt{e} + \cot(dx+c) \sqrt{e} - \sqrt{2} \sqrt{e \cot(dx+c)}) \sqrt{2}}{4(a^2+b^2)^3 d} \\ & + \frac{(a+b) (a^2-4ab+b^2) e^{9/2} \ln(\sqrt{e} + \cot(dx+c) \sqrt{e} + \sqrt{2} \sqrt{e \cot(dx+c)}) \sqrt{2}}{4(a^2+b^2)^3 d} - \frac{(15a^4+31a^2b^2+8b^4) e^4 \sqrt{e \cot(dx+c)}}{4b^3 (a^2+b^2)^2 d} \end{aligned}$$

Result (type 3, 1253 leaves):

$$\begin{aligned} & - \frac{2e^4 \sqrt{e \cot(dx+c)}}{db^3} - \frac{9e^5 a^7 (e \cot(dx+c))^3/2}{4db^2 (a^2+b^2)^3 (e \cot(dx+c) b + ae)^2} - \frac{13e^5 a^5 (e \cot(dx+c))^3/2}{2d (a^2+b^2)^3 (e \cot(dx+c) b + ae)^2} - \frac{17e^5 a^3 b^2 (e \cot(dx+c))^3/2}{4d (a^2+b^2)^3 (e \cot(dx+c) b + ae)^2} \\ & - \frac{7e^6 a^8 \sqrt{e \cot(dx+c)}}{4db^3 (a^2+b^2)^3 (e \cot(dx+c) b + ae)^2} - \frac{11e^6 a^6 \sqrt{e \cot(dx+c)}}{2db (a^2+b^2)^3 (e \cot(dx+c) b + ae)^2} - \frac{15e^6 a^4 b \sqrt{e \cot(dx+c)}}{4d (a^2+b^2)^3 (e \cot(dx+c) b + ae)^2} \\ & + \frac{15e^5 a^7 \arctan\left(\frac{\sqrt{e \cot(dx+c)} b}{\sqrt{aeb}}\right)}{4db^3 (a^2+b^2)^3 \sqrt{aeb}} + \frac{23e^5 a^5 \arctan\left(\frac{\sqrt{e \cot(dx+c)} b}{\sqrt{aeb}}\right)}{2db (a^2+b^2)^3 \sqrt{aeb}} + \frac{63e^5 a^3 b \arctan\left(\frac{\sqrt{e \cot(dx+c)} b}{\sqrt{aeb}}\right)}{4d (a^2+b^2)^3 \sqrt{aeb}} \\ & - \frac{3e^4 (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2 b}{2d (a^2+b^2)^3} + \frac{e^4 (e^2)^{1/4} \sqrt{2} \arctan\left(\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^3}{2d (a^2+b^2)^3} \\ & + \frac{3e^4 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) a^2 b}{2d (a^2+b^2)^3} - \frac{e^4 (e^2)^{1/4} \sqrt{2} \arctan\left(-\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1\right) b^3}{2d (a^2+b^2)^3} \\ & - \frac{3e^4 (e^2)^{1/4} \sqrt{2} \ln\left(\frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}\right) a^2 b}{4d (a^2+b^2)^3} \end{aligned}$$

$$\begin{aligned}
& + \frac{e^4 (e^2)^{1/4} \sqrt{2} \ln \left( \frac{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}} \right) b^3}{4d(a^2+b^2)^3} \\
& - \frac{e^5 \sqrt{2} \ln \left( \frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}} \right) a^3}{4d(a^2+b^2)^3 (e^2)^{1/4}} + \frac{3e^5 \sqrt{2} \ln \left( \frac{e \cot(dx+c) - (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}}{e \cot(dx+c) + (e^2)^{1/4} \sqrt{e \cot(dx+c)} \sqrt{2} + \sqrt{e^2}} \right) a b^2}{4d(a^2+b^2)^3 (e^2)^{1/4}} \\
& - \frac{e^5 \sqrt{2} \arctan \left( \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) a^3}{2d(a^2+b^2)^3 (e^2)^{1/4}} + \frac{3e^5 \sqrt{2} \arctan \left( \frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) a b^2}{2d(a^2+b^2)^3 (e^2)^{1/4}} + \frac{e^5 \sqrt{2} \arctan \left( -\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) a^3}{2d(a^2+b^2)^3 (e^2)^{1/4}} \\
& - \frac{3e^5 \sqrt{2} \arctan \left( -\frac{\sqrt{2} \sqrt{e \cot(dx+c)}}{(e^2)^{1/4}} + 1 \right) a b^2}{2d(a^2+b^2)^3 (e^2)^{1/4}}
\end{aligned}$$

Problem 26: Result more than twice size of optimal antiderivative.

$$\int \frac{1 - \text{I} \cot(dx+c)}{\sqrt{a+b \cot(dx+c)}} dx$$

Optimal (type 3, 36 leaves, 3 steps):

$$\frac{-2 \text{I} \operatorname{arctanh} \left( \frac{\sqrt{a+b \cot(dx+c)}}{\sqrt{b+a}} \right)}{d \sqrt{b+a}}$$

Result (type 3, 1621 leaves):

$$\begin{aligned}
& \frac{\text{I} \ln \left( \sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2} \right) a b^2}{d \sqrt{2\sqrt{a^2+b^2}+2a} \sqrt{a^2+b^2} (\sqrt{a^2+b^2} a + a^2 + b^2)} \\
& - \frac{\text{I} \ln \left( b \cot(dx+c) + a + \sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} + \sqrt{a^2+b^2} \right) a}{2d \sqrt{2\sqrt{a^2+b^2}+2a} \sqrt{a^2+b^2}} \\
& + \frac{\text{I} \ln \left( \sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2} \right) b^2}{2d \sqrt{2\sqrt{a^2+b^2}+2a} (\sqrt{a^2+b^2} a + a^2 + b^2)} \\
& - \frac{\text{I} \ln \left( b \cot(dx+c) + a + \sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} + \sqrt{a^2+b^2} \right)}{2d \sqrt{2\sqrt{a^2+b^2}+2a}}
\end{aligned}$$

$$\begin{aligned}
& + \frac{\ln\left(\sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2}\right) ab}{2d\sqrt{2\sqrt{a^2+b^2}+2a} (\sqrt{a^2+b^2} a + a^2 + b^2)} \\
& + \frac{\ln\left(\sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2}\right) a^2 b}{2d\sqrt{2\sqrt{a^2+b^2}+2a} \sqrt{a^2+b^2} (\sqrt{a^2+b^2} a + a^2 + b^2)} \\
& + \frac{\ln\left(\sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2}\right) b^3}{2d\sqrt{2\sqrt{a^2+b^2}+2a} \sqrt{a^2+b^2} (\sqrt{a^2+b^2} a + a^2 + b^2)} \\
& + \frac{\ln\left(\sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2}\right) a^2}{d\sqrt{2\sqrt{a^2+b^2}+2a} (\sqrt{a^2+b^2} a + a^2 + b^2)} + \frac{\arctan\left(\frac{\sqrt{2\sqrt{a^2+b^2}+2a} - 2\sqrt{a+b \cot(dx+c)}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right) ab}{d(\sqrt{a^2+b^2} a + a^2 + b^2) \sqrt{2\sqrt{a^2+b^2}-2a}} \\
& + \frac{\arctan\left(\frac{\sqrt{2\sqrt{a^2+b^2}+2a} - 2\sqrt{a+b \cot(dx+c)}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right) a^2 b}{d\sqrt{a^2+b^2} (\sqrt{a^2+b^2} a + a^2 + b^2) \sqrt{2\sqrt{a^2+b^2}-2a}} + \frac{\arctan\left(\frac{\sqrt{2\sqrt{a^2+b^2}+2a} - 2\sqrt{a+b \cot(dx+c)}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right) b^3}{d\sqrt{a^2+b^2} (\sqrt{a^2+b^2} a + a^2 + b^2) \sqrt{2\sqrt{a^2+b^2}-2a}} \\
& + \frac{\ln\left(\sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} - b \cot(dx+c) - a - \sqrt{a^2+b^2}\right) a^3}{d\sqrt{2\sqrt{a^2+b^2}+2a} \sqrt{a^2+b^2} (\sqrt{a^2+b^2} a + a^2 + b^2)} + \frac{\text{I arctan}\left(\frac{2\sqrt{a+b \cot(dx+c)} + \sqrt{2\sqrt{a^2+b^2}+2a}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right)}{d\sqrt{2\sqrt{a^2+b^2}-2a}} \\
& - \frac{\ln\left(b \cot(dx+c) + a + \sqrt{a+b \cot(dx+c)} \sqrt{2\sqrt{a^2+b^2}+2a} + \sqrt{a^2+b^2}\right) b}{2d\sqrt{2\sqrt{a^2+b^2}+2a} \sqrt{a^2+b^2}} - \frac{\text{I arctan}\left(\frac{\sqrt{2\sqrt{a^2+b^2}+2a} - 2\sqrt{a+b \cot(dx+c)}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right) b^2}{d(\sqrt{a^2+b^2} a + a^2 + b^2) \sqrt{2\sqrt{a^2+b^2}-2a}} \\
& - \frac{\text{I arctan}\left(\frac{2\sqrt{a+b \cot(dx+c)} + \sqrt{2\sqrt{a^2+b^2}+2a}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right) a}{d\sqrt{a^2+b^2} \sqrt{2\sqrt{a^2+b^2}-2a}} - \frac{\arctan\left(\frac{2\sqrt{a+b \cot(dx+c)} + \sqrt{2\sqrt{a^2+b^2}+2a}}{\sqrt{2\sqrt{a^2+b^2}-2a}}\right) b}{d\sqrt{a^2+b^2} \sqrt{2\sqrt{a^2+b^2}-2a}}
\end{aligned}$$

Problem 27: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \cot(dx+c)}{a + b \cot(dx+c)} dx$$

Optimal(type 3, 59 leaves, 2 steps):

$$\frac{(Aa + Bb)x}{a^2 + b^2} - \frac{(Ab - Ba) \ln(b \cos(dx + c) + a \sin(dx + c))}{d(a^2 + b^2)}$$

Result(type 3, 186 leaves):

$$\begin{aligned} & \frac{\ln(\cot(dx + c)^2 + 1) Ab}{2d(a^2 + b^2)} - \frac{\ln(\cot(dx + c)^2 + 1) Ba}{2d(a^2 + b^2)} - \frac{A\pi a}{2d(a^2 + b^2)} - \frac{B\pi b}{2d(a^2 + b^2)} + \frac{A \operatorname{arccot}(\cot(dx + c)) a}{d(a^2 + b^2)} + \frac{B \operatorname{arccot}(\cot(dx + c)) b}{d(a^2 + b^2)} \\ & - \frac{\ln(a + b \cot(dx + c)) Ab}{d(a^2 + b^2)} + \frac{\ln(a + b \cot(dx + c)) Ba}{d(a^2 + b^2)} \end{aligned}$$

Problem 28: Result more than twice size of optimal antiderivative.

$$\int (b \cot(dx + c) - a) \sqrt{a + b \cot(dx + c)} dx$$

Optimal(type 3, 341 leaves, 13 steps):

$$\begin{aligned} & - \frac{2b\sqrt{a + b \cot(dx + c)}}{d} + \frac{b \operatorname{arctanh}\left(\frac{-\sqrt{2}\sqrt{a + b \cot(dx + c)} + \sqrt{a + \sqrt{a^2 + b^2}}}{\sqrt{a - \sqrt{a^2 + b^2}}}\right) \sqrt{a^2 + b^2} \sqrt{2}}{2d\sqrt{a - \sqrt{a^2 + b^2}}} \\ & - \frac{b \operatorname{arctanh}\left(\frac{\sqrt{2}\sqrt{a + b \cot(dx + c)} + \sqrt{a + \sqrt{a^2 + b^2}}}{\sqrt{a - \sqrt{a^2 + b^2}}}\right) \sqrt{a^2 + b^2} \sqrt{2}}{2d\sqrt{a - \sqrt{a^2 + b^2}}} \\ & - \frac{b \ln\left(a + b \cot(dx + c) + \sqrt{a^2 + b^2} - \sqrt{2}\sqrt{a + b \cot(dx + c)}\sqrt{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2} \sqrt{2}}{4d\sqrt{a + \sqrt{a^2 + b^2}}} \\ & + \frac{b \ln\left(a + b \cot(dx + c) + \sqrt{a^2 + b^2} + \sqrt{2}\sqrt{a + b \cot(dx + c)}\sqrt{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2} \sqrt{2}}{4d\sqrt{a + \sqrt{a^2 + b^2}}} \end{aligned}$$

Result(type ?, 2284 leaves): Display of huge result suppressed!

Problem 29: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \cot(dx + c)}{\sqrt{a + b \cot(dx + c)}} dx$$

Optimal(type 3, 84 leaves, 7 steps):

$$\frac{(IA + B) \operatorname{arctanh}\left(\frac{\sqrt{a + b \cot(dx + c)}}{\sqrt{a - Ib}}\right)}{d\sqrt{a - Ib}} - \frac{(IA - B) \operatorname{arctanh}\left(\frac{\sqrt{a + b \cot(dx + c)}}{\sqrt{Ib + a}}\right)}{d\sqrt{Ib + a}}$$

Result(type ?, 3975 leaves): Display of huge result suppressed!

Problem 30: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \cot(dx + c)}{(a + b \cot(dx + c))^3 / 2} dx$$

Optimal(type 3, 118 leaves, 8 steps):

$$\frac{(IA + B) \operatorname{arctanh}\left(\frac{\sqrt{a + b \cot(dx + c)}}{\sqrt{a - Ib}}\right)}{(a - Ib)^3 / 2 d} - \frac{(IA - B) \operatorname{arctanh}\left(\frac{\sqrt{a + b \cot(dx + c)}}{\sqrt{Ib + a}}\right)}{(Ib + a)^3 / 2 d} + \frac{2(Ab - Ba)}{(a^2 + b^2) d \sqrt{a + b \cot(dx + c)}}$$

Result(type ?, 7950 leaves): Display of huge result suppressed!

Test results for the 20 problems in "4.4.7 (d trig)^m (a+b (c cot)^n)^p.txt"

Problem 1: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + C \cot(dx + c)^2}{\sqrt{b \tan(dx + c)}} dx$$

Optimal(type 3, 182 leaves, 15 steps):

$$\begin{aligned} & - \frac{(A - C) \arctan\left(1 - \frac{\sqrt{2} \sqrt{b \tan(dx + c)}}{\sqrt{b}}\right) \sqrt{2}}{2d\sqrt{b}} + \frac{(A - C) \arctan\left(1 + \frac{\sqrt{2} \sqrt{b \tan(dx + c)}}{\sqrt{b}}\right) \sqrt{2}}{2d\sqrt{b}} \\ & - \frac{(A - C) \ln\left(\sqrt{b} - \sqrt{2} \sqrt{b \tan(dx + c)} + \sqrt{b} \tan(dx + c)\right) \sqrt{2}}{4d\sqrt{b}} + \frac{(A - C) \ln\left(\sqrt{b} + \sqrt{2} \sqrt{b \tan(dx + c)} + \sqrt{b} \tan(dx + c)\right) \sqrt{2}}{4d\sqrt{b}} \\ & - \frac{2bC}{3d(b \tan(dx + c))^3 / 2} \end{aligned}$$

Result(type ?, 2493 leaves): Display of huge result suppressed!

Problem 3: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + b \cot(dx + c)^2)^3} dx$$

Optimal(type 3, 136 leaves, 6 steps):



$$\frac{x}{(a-b)^3} + \frac{b \cot(dx+c)}{4a(a-b)d(a+b \cot(dx+c))^2} + \frac{(7a-3b)b \cot(dx+c)}{8a^2(a-b)^2d(a+b \cot(dx+c))^2} + \frac{(15a^2-10ab+3b^2) \arctan\left(\frac{\cot(dx+c)\sqrt{b}}{\sqrt{a}}\right)\sqrt{b}}{8a^{5/2}(a-b)^3d}$$

Result(type 3, 362 leaves):

$$\begin{aligned} & \frac{7b^2 \cot(dx+c)^3}{8d(a-b)^3(a+b \cot(dx+c))^2} - \frac{5b^3 \cot(dx+c)^3}{4d(a-b)^3(a+b \cot(dx+c))^2a} + \frac{3b^4 \cot(dx+c)^3}{8d(a-b)^3(a+b \cot(dx+c))^2a^2} \\ & + \frac{9ba \cot(dx+c)}{8d(a-b)^3(a+b \cot(dx+c))^2} - \frac{7b^2 \cot(dx+c)}{4d(a-b)^3(a+b \cot(dx+c))^2} + \frac{5b^3 \cot(dx+c)}{8d(a-b)^3(a+b \cot(dx+c))^2a} + \frac{15b \arctan\left(\frac{\cot(dx+c)b}{\sqrt{ab}}\right)}{8d(a-b)^3\sqrt{ab}} \\ & - \frac{5b^2 \arctan\left(\frac{\cot(dx+c)b}{\sqrt{ab}}\right)}{4d(a-b)^3a\sqrt{ab}} + \frac{3b^3 \arctan\left(\frac{\cot(dx+c)b}{\sqrt{ab}}\right)}{8d(a-b)^3a^2\sqrt{ab}} - \frac{\pi}{2d(a-b)^3} + \frac{\operatorname{arccot}(\cot(dx+c))}{d(a-b)^3} \end{aligned}$$

Problem 10: Result more than twice size of optimal antiderivative.

$$\int \sqrt{a+b \cot(x)^2} dx$$

Optimal(type 3, 53 leaves, 6 steps):

$$-\arctan\left(\frac{\cot(x)\sqrt{a-b}}{\sqrt{a+b \cot(x)^2}}\right)\sqrt{a-b} - \operatorname{arctanh}\left(\frac{\cot(x)\sqrt{b}}{\sqrt{a+b \cot(x)^2}}\right)\sqrt{b}$$

Result(type 3, 136 leaves):

$$-\sqrt{b} \ln(\cot(x)\sqrt{b} + \sqrt{a+b \cot(x)^2}) + \frac{\sqrt{b^4(a-b)} \arctan\left(\frac{b^2(a-b)\cot(x)}{\sqrt{b^4(a-b)}\sqrt{a+b \cot(x)^2}}\right)}{b(a-b)} - \frac{a\sqrt{b^4(a-b)} \arctan\left(\frac{b^2(a-b)\cot(x)}{\sqrt{b^4(a-b)}\sqrt{a+b \cot(x)^2}}\right)}{b^2(a-b)}$$

Problem 11: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (a+b \cot(x)^2)^{3/2} \tan(x) dx$$

Optimal(type 3, 61 leaves, 8 steps):

$$a^{3/2} \operatorname{arctanh}\left(\frac{\sqrt{a+b \cot(x)^2}}{\sqrt{a}}\right) - (a-b)^{3/2} \operatorname{arctanh}\left(\frac{\sqrt{a+b \cot(x)^2}}{\sqrt{a-b}}\right) - b\sqrt{a+b \cot(x)^2}$$

Result(type ?, 2627 leaves): Display of huge result suppressed!

Problem 16: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\tan(x)}{\sqrt{a + b \cot(x)^2}} dx$$

Optimal(type 3, 48 leaves, 7 steps):

$$\frac{\operatorname{arctanh}\left(\frac{\sqrt{a + b \cot(x)^2}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{\operatorname{arctanh}\left(\frac{\sqrt{a + b \cot(x)^2}}{\sqrt{a - b}}\right)}{\sqrt{a - b}}$$

Result(type 4, 375 leaves):

$$\frac{1}{\sqrt{\frac{2\sqrt{a}\sqrt{a-b}-2a+b}{b}} \sqrt{\frac{a \cos(x)^2 - b \cos(x)^2 - a}{\cos(x)^2 - 1}} (\cos(x) - 1)} \left( 2\sqrt{2} \sqrt{\frac{\cos(x) \sqrt{a-b} \sqrt{a} - \sqrt{a} \sqrt{a-b} - \cos(x) a + b \cos(x) + a}{b (\cos(x) + 1)}} \right.$$

$$\left. \sqrt{-\frac{2 (\cos(x) \sqrt{a-b} \sqrt{a} - \sqrt{a} \sqrt{a-b} + \cos(x) a - b \cos(x) - a)}{b (\cos(x) + 1)}} \right) \left( -\operatorname{EllipticPi}\left(\frac{(\cos(x) - 1) \sqrt{\frac{2\sqrt{a}\sqrt{a-b}-2a+b}{b}}}{\sin(x)}\right), \right.$$

$$\left. \frac{b}{2\sqrt{a}\sqrt{a-b}-2a+b}, \sqrt{\frac{-\frac{2\sqrt{a}\sqrt{a-b}+2a-b}{b}}{\frac{2\sqrt{a}\sqrt{a-b}-2a+b}{b}}} \right) + \operatorname{EllipticPi}\left(\frac{(\cos(x) - 1) \sqrt{\frac{2\sqrt{a}\sqrt{a-b}-2a+b}{b}}}{\sin(x)}, -\frac{b}{2\sqrt{a}\sqrt{a-b}-2a+b}, \right.$$

$$\left. \left. \frac{\sqrt{\frac{-\frac{2\sqrt{a}\sqrt{a-b}+2a-b}{b}}{\frac{2\sqrt{a}\sqrt{a-b}-2a+b}{b}}}}{\sqrt{\frac{2\sqrt{a}\sqrt{a-b}-2a+b}{b}}} \right) \right) \sin(x)$$

Problem 20: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot(x)}{(a + b \cot(x)^4)^{5/2}} dx$$

Optimal(type 3, 105 leaves, 7 steps):

$$\frac{\operatorname{arctanh}\left(\frac{a - b \cot(x)^2}{\sqrt{a + b} \sqrt{a + b \cot(x)^4}}\right)}{2(a + b)^{5/2}} + \frac{-a - b \cot(x)^2}{6a(a + b)(a + b \cot(x)^4)^{3/2}} + \frac{-3a^2 - b(5a + 2b) \cot(x)^2}{6a^2(a + b)^2 \sqrt{a + b \cot(x)^4}}$$

Result(type 3, 601 leaves):

$$\begin{aligned}
& b^2 \ln \left( \frac{2a + 2b - 2(\cot(x)^2 + 1)b + 2\sqrt{a+b}\sqrt{b(\cot(x)^2 + 1)^2 - 2(\cot(x)^2 + 1)b + a + b}}{\cot(x)^2 + 1} \right) \\
& - \frac{2(\sqrt{-ab} + b)^2(\sqrt{-ab} - b)^2\sqrt{a+b}}{\sqrt{b\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)^2 + 2\sqrt{-ab}\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)}} - \frac{\sqrt{b\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)^2 + 2\sqrt{-ab}\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)}}{24(\sqrt{-ab} + b)a\sqrt{-ab}\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)^2} \\
& - \frac{\sqrt{b\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)^2 - 2\sqrt{-ab}\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)}}{24(\sqrt{-ab} - b)a\sqrt{-ab}\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)^2} + \frac{\sqrt{b\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)^2 - 2\sqrt{-ab}\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)}}{24(\sqrt{-ab} - b)a^2\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)} \\
& + \frac{(2\sqrt{-ab} - b)\sqrt{b\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)^2 - 2\sqrt{-ab}\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)}}{8(\sqrt{-ab} - b)^2a^2\left(\cot(x)^2 + \frac{\sqrt{-ab}}{b}\right)} \\
& - \frac{(2\sqrt{-ab} + b)\sqrt{b\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)^2 + 2\sqrt{-ab}\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)}}{8(\sqrt{-ab} + b)^2a^2\left(\cot(x)^2 - \frac{\sqrt{-ab}}{b}\right)}
\end{aligned}$$

Test results for the 11 problems in "4.4.9 trig^m (a+b cot^n+c cot^(2 n))^p.txt"

Problem 1: Humongous result has more than 20000 leaves.

$$\int \frac{\cot(ex+d)^5}{\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}} dx$$

Optimal (type 3, 484 leaves, 15 steps):

$$\begin{aligned}
& - \frac{b \operatorname{arctanh}\left(\frac{b+2c\cot(ex+d)}{2\sqrt{c}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{2c^3/2e} + \frac{b(-12ac+5b^2) \operatorname{arctanh}\left(\frac{b+2c\cot(ex+d)}{2\sqrt{c}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{16c^7/2e} \\
& + \frac{\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}{ce} - \frac{\cot(ex+d)^2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}{3ce} \\
& - \frac{(15b^2-16ac-10bcc\cot(ex+d))\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}{24c^3e}
\end{aligned}$$

$$\begin{aligned}
& - \frac{\operatorname{arctanh}\left(\frac{(a-c+b\cot(ex+d)-\sqrt{a^2-2ac+b^2+c^2})\sqrt{2}}{2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}\sqrt{a-c-\sqrt{a^2-2ac+b^2+c^2}}}\right)\sqrt{a-c-\sqrt{a^2-2ac+b^2+c^2}}\sqrt{2}}{2e\sqrt{a^2-2ac+b^2+c^2}} \\
& + \frac{\operatorname{arctanh}\left(\frac{(a-c+b\cot(ex+d)+\sqrt{a^2-2ac+b^2+c^2})\sqrt{2}}{2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}\sqrt{a-c+\sqrt{a^2-2ac+b^2+c^2}}}\right)\sqrt{a-c+\sqrt{a^2-2ac+b^2+c^2}}\sqrt{2}}{2e\sqrt{a^2-2ac+b^2+c^2}}
\end{aligned}$$

Result(type ?, 9581342 leaves): Display of huge result suppressed!

Problem 2: Humongous result has more than 20000 leaves.

$$\int \frac{\cot(ex+d)}{\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}} dx$$

Optimal(type 3, 261 leaves, 6 steps):

$$\begin{aligned}
& - \frac{\operatorname{arctanh}\left(\frac{(a-c+b\cot(ex+d)-\sqrt{a^2-2ac+b^2+c^2})\sqrt{2}}{2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}\sqrt{a-c-\sqrt{a^2-2ac+b^2+c^2}}}\right)\sqrt{a-c-\sqrt{a^2-2ac+b^2+c^2}}\sqrt{2}}{2e\sqrt{a^2-2ac+b^2+c^2}} \\
& + \frac{\operatorname{arctanh}\left(\frac{(a-c+b\cot(ex+d)+\sqrt{a^2-2ac+b^2+c^2})\sqrt{2}}{2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}\sqrt{a-c+\sqrt{a^2-2ac+b^2+c^2}}}\right)\sqrt{a-c+\sqrt{a^2-2ac+b^2+c^2}}\sqrt{2}}{2e\sqrt{a^2-2ac+b^2+c^2}}
\end{aligned}$$

Result(type ?, 9338542 leaves): Display of huge result suppressed!

Problem 3: Humongous result has more than 20000 leaves.

$$\int \cot(ex+d)^3 \sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2} dx$$

Optimal(type 3, 668 leaves, 16 steps):

$$\begin{aligned}
& - \frac{b(-4ac+b^2)\operatorname{arctanh}\left(\frac{b+2c\cot(ex+d)}{2\sqrt{c}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{16c^5/2e} - \frac{(a+b\cot(ex+d)+c\cot(ex+d)^2)^{3/2}}{3ce} \\
& + \frac{b\operatorname{arctanh}\left(\frac{b+2c\cot(ex+d)}{2\sqrt{c}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{2e\sqrt{c}} + \frac{\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}{e} \\
& + \frac{b(b+2c\cot(ex+d))\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}{8c^2e}
\end{aligned}$$

$$\begin{aligned}
& - \frac{1}{2(a^2 - 2ac + b^2 + c^2)^{1/4} e} \left( \operatorname{arctanh} \left( \left( (b^2 + b \cot(ex + d) \sqrt{a^2 - 2ac + b^2 + c^2} + (a - c) (a - c + \sqrt{a^2 - 2ac + b^2 + c^2})) \sqrt{2} \right) \right) \right) / \\
& \left( 2(a^2 - 2ac + b^2 + c^2)^{1/4} \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \sqrt{a^2 + b^2 + c^2} (c - \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c - \sqrt{a^2 - 2ac + b^2 + c^2}) \right) / \\
& \sqrt{a^2 + b^2 + c^2} (c - \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c - \sqrt{a^2 - 2ac + b^2 + c^2}) \sqrt{2} \\
& + \frac{1}{2(a^2 - 2ac + b^2 + c^2)^{1/4} e} \left( \operatorname{arctan} \left( \left( (b^2 + (a - c) (a - c - \sqrt{a^2 - 2ac + b^2 + c^2}) - b \cot(ex + d) \sqrt{a^2 - 2ac + b^2 + c^2}) \sqrt{2} \right) \right) \right) / \\
& \left( 2(a^2 - 2ac + b^2 + c^2)^{1/4} \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \sqrt{a^2 + b^2 + c^2} (c + \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c + \sqrt{a^2 - 2ac + b^2 + c^2}) \right) / \\
& \sqrt{a^2 + b^2 + c^2} (c + \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c + \sqrt{a^2 - 2ac + b^2 + c^2}) \sqrt{2}
\end{aligned}$$

Result(type ?, 17766957 leaves): Display of huge result suppressed!

Problem 4: Humongous result has more than 20000 leaves.

$$\int \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \tan(ex + d)^3 dx$$

Optimal(type 3, 620 leaves, 21 steps):

$$\begin{aligned}
& \frac{(-4ac + b^2) \operatorname{arctanh} \left( \frac{2a + b \cot(ex + d)}{2\sqrt{a} \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2}} \right) - \operatorname{arctanh} \left( \frac{2a + b \cot(ex + d)}{2\sqrt{a} \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2}} \right) \sqrt{a}}{8a^3/2e} \\
& + \frac{1}{2(a^2 - 2ac + b^2 + c^2)^{1/4} e} \left( \operatorname{arctanh} \left( \left( (b^2 + b \cot(ex + d) \sqrt{a^2 - 2ac + b^2 + c^2} + (a - c) (a - c + \sqrt{a^2 - 2ac + b^2 + c^2})) \sqrt{2} \right) \right) \right) / \\
& \left( 2(a^2 - 2ac + b^2 + c^2)^{1/4} \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \sqrt{a^2 + b^2 + c^2} (c - \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c - \sqrt{a^2 - 2ac + b^2 + c^2}) \right) / \\
& \sqrt{a^2 + b^2 + c^2} (c - \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c - \sqrt{a^2 - 2ac + b^2 + c^2}) \sqrt{2} \\
& - \frac{1}{2(a^2 - 2ac + b^2 + c^2)^{1/4} e} \left( \operatorname{arctan} \left( \left( (b^2 + (a - c) (a - c - \sqrt{a^2 - 2ac + b^2 + c^2}) - b \cot(ex + d) \sqrt{a^2 - 2ac + b^2 + c^2}) \sqrt{2} \right) \right) \right) / \\
& \left( 2(a^2 - 2ac + b^2 + c^2)^{1/4} \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \sqrt{a^2 + b^2 + c^2} (c + \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c + \sqrt{a^2 - 2ac + b^2 + c^2}) \right) / \\
& \sqrt{a^2 + b^2 + c^2} (c + \sqrt{a^2 - 2ac + b^2 + c^2}) - a(2c + \sqrt{a^2 - 2ac + b^2 + c^2}) \sqrt{2} \\
& + \frac{(2a + b \cot(ex + d)) \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \tan(ex + d)^2}{4ae}
\end{aligned}$$

Result(type ?, 2698877 leaves): Display of huge result suppressed!

Problem 5: Humongous result has more than 20000 leaves.

$$\int \frac{\tan(ex+d)}{(a+b\cot(ex+d)+c\cot(ex+d)^2)^{3/2}} dx$$

Optimal (type 3, 684 leaves, 13 steps):

$$\frac{\operatorname{arctanh}\left(\frac{2a+b\cot(ex+d)}{2\sqrt{a}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{a^{3/2}e} - \frac{2(b^2-2ac+bc\cot(ex+d))}{a(-4ac+b^2)e\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}$$

$$+ \frac{2(a(b^2-2(a-c)c)+bc(a+c)\cot(ex+d))}{(b^2+(a-c)^2)(-4ac+b^2)e\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}$$

$$- \frac{1}{2(a^2-2ac+b^2+c^2)^{3/2}e} \left( \operatorname{arctanh}\left(\left(\left(b^2-(a-c)(a-c-\sqrt{a^2-2ac+b^2+c^2})-bc\cot(ex+d)(2a-2c\right.\right.\right.\right.$$

$$\left.\left.\left.\left.+ \sqrt{a^2-2ac+b^2+c^2}\right)\right)\sqrt{2}\right) / \right.$$

$$\left. \left(2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}\sqrt{2a-2c+\sqrt{a^2-2ac+b^2+c^2}}\sqrt{a^2-b^2-2ac+c^2-(a-c)\sqrt{a^2-2ac+b^2+c^2}}\right) \right.$$

$$\left. \sqrt{2a-2c+\sqrt{a^2-2ac+b^2+c^2}}\sqrt{a^2-b^2-2ac+c^2-(a-c)\sqrt{a^2-2ac+b^2+c^2}}\sqrt{2}\right)$$

$$+ \frac{1}{2(a^2-2ac+b^2+c^2)^{3/2}e} \left( \operatorname{arctanh}\left(\left(\left(b^2-b\cot(ex+d)(2a-2c-\sqrt{a^2-2ac+b^2+c^2})-(a-c)(a-c\right.\right.\right.\right.$$

$$\left.\left.\left.\left.+ \sqrt{a^2-2ac+b^2+c^2}\right)\right)\sqrt{2}\right) / \right.$$

$$\left. \left(2\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}\sqrt{2a-2c-\sqrt{a^2-2ac+b^2+c^2}}\sqrt{a^2-b^2-2ac+c^2+(a-c)\sqrt{a^2-2ac+b^2+c^2}}\right) \right.$$

$$\left. \sqrt{2a-2c-\sqrt{a^2-2ac+b^2+c^2}}\sqrt{a^2-b^2-2ac+c^2+(a-c)\sqrt{a^2-2ac+b^2+c^2}}\sqrt{2}\right)$$

Result (type ?, 21253698 leaves): Display of huge result suppressed!

Problem 6: Attempted integration timed out after 120 seconds.

$$\int \frac{\tan(ex+d)^3}{(a+b\cot(ex+d)+c\cot(ex+d)^2)^{3/2}} dx$$

Optimal (type 3, 923 leaves, 18 steps):

$$\frac{\operatorname{arctanh}\left(\frac{2a+b\cot(ex+d)}{2\sqrt{a}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{a^{3/2}e} + \frac{3(-4ac+5b^2)\operatorname{arctanh}\left(\frac{2a+b\cot(ex+d)}{2\sqrt{a}\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}\right)}{8a^{7/2}e}$$

$$+ \frac{2(b^2-2ac+bc\cot(ex+d))}{a(-4ac+b^2)e\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}} - \frac{2(a(b^2-2(a-c)c)+bc(a+c)\cot(ex+d))}{(b^2+(a-c)^2)(-4ac+b^2)e\sqrt{a+b\cot(ex+d)+c\cot(ex+d)^2}}$$

$$+ \frac{1}{2(a^2-2ac+b^2+c^2)^{3/2}e} \left( \operatorname{arctanh}\left(\left(\left(b^2-(a-c)(a-c-\sqrt{a^2-2ac+b^2+c^2})-bc\cot(ex+d)(2a-2c\right.\right.\right.\right.$$

$$\begin{aligned}
& + \sqrt{a^2 - 2ac + b^2 + c^2} \Big) \sqrt{2} \Big) / \\
& \left( 2\sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \sqrt{2a - 2c + \sqrt{a^2 - 2ac + b^2 + c^2}} \sqrt{a^2 - b^2 - 2ac + c^2 - (a - c) \sqrt{a^2 - 2ac + b^2 + c^2}} \right) \\
& \sqrt{2a - 2c + \sqrt{a^2 - 2ac + b^2 + c^2}} \sqrt{a^2 - b^2 - 2ac + c^2 - (a - c) \sqrt{a^2 - 2ac + b^2 + c^2}} \sqrt{2} \Big) \\
& - \frac{1}{2(a^2 - 2ac + b^2 + c^2)^{3/2} e} \left( \operatorname{arctanh} \left( \left( (b^2 - b \cot(ex + d) (2a - 2c - \sqrt{a^2 - 2ac + b^2 + c^2}) - (a - c) (a - c \right. \right. \right. \\
& \left. \left. \left. + \sqrt{a^2 - 2ac + b^2 + c^2} \right) \sqrt{2} \right) \right) / \\
& \left( 2\sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \sqrt{2a - 2c - \sqrt{a^2 - 2ac + b^2 + c^2}} \sqrt{a^2 - b^2 - 2ac + c^2 + (a - c) \sqrt{a^2 - 2ac + b^2 + c^2}} \right) \\
& \sqrt{2a - 2c - \sqrt{a^2 - 2ac + b^2 + c^2}} \sqrt{a^2 - b^2 - 2ac + c^2 + (a - c) \sqrt{a^2 - 2ac + b^2 + c^2}} \sqrt{2} \Big) \\
& - \frac{b(-52ac + 15b^2) \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \tan(ex + d)}{4a^3(-4ac + b^2)e} - \frac{2(b^2 - 2ac + bc \cot(ex + d)) \tan(ex + d)^2}{a(-4ac + b^2)e \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2}} \\
& + \frac{(-12ac + 5b^2) \sqrt{a + b \cot(ex + d) + c \cot(ex + d)^2} \tan(ex + d)^2}{2a^2(-4ac + b^2)e}
\end{aligned}$$

Result(type 1, 1 leaves):???

Problem 10: Result more than twice size of optimal antiderivative.

$$\int \cot(ex + d)^3 \sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4} dx$$

Optimal(type 3, 185 leaves, 8 steps):

$$\begin{aligned}
& \frac{(b^2 + 4bc - 4c(a + 2c)) \operatorname{arctanh} \left( \frac{b + 2c \cot(ex + d)^2}{2\sqrt{c} \sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4}} \right)}{16c^3 \sqrt{2} e} \\
& - \frac{\operatorname{arctanh} \left( \frac{2a - b + (b - 2c) \cot(ex + d)^2}{2\sqrt{a - b + c} \sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4}} \right) \sqrt{a - b + c}}{2e} - \frac{(b - 4c + 2c \cot(ex + d)^2) \sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4}}{8ce}
\end{aligned}$$

Result(type 3, 466 leaves):

$$\begin{aligned}
& - \frac{\sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4} \cot(ex + d)^2}{4e} - \frac{\sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4} b}{8ec} \\
& - \frac{\ln \left( \frac{\frac{b}{2} + c \cot(ex + d)^2}{\sqrt{c}} + \sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4} \right) a}{4e\sqrt{c}} + \frac{\ln \left( \frac{\frac{b}{2} + c \cot(ex + d)^2}{\sqrt{c}} + \sqrt{a + b \cot(ex + d)^2 + c \cot(ex + d)^4} \right) b^2}{16ec^3 \sqrt{2}}
\end{aligned}$$

$$\begin{aligned}
& + \frac{\sqrt{(\cot(ex+d)^2+1)^2 c + (b-2c)(\cot(ex+d)^2+1) + a-b+c}}{2e} \\
& + \frac{\ln\left(\frac{\frac{b}{2} - c + c(\cot(ex+d)^2+1)}{\sqrt{c}} + \sqrt{(\cot(ex+d)^2+1)^2 c + (b-2c)(\cot(ex+d)^2+1) + a-b+c}\right) b}{4e\sqrt{c}} \\
& - \frac{\ln\left(\frac{\frac{b}{2} - c + c(\cot(ex+d)^2+1)}{\sqrt{c}} + \sqrt{(\cot(ex+d)^2+1)^2 c + (b-2c)(\cot(ex+d)^2+1) + a-b+c}\right) \sqrt{c}}{2e} \\
& - \frac{1}{2e} \left( \sqrt{a-b+c} \ln\left(\frac{1}{\cot(ex+d)^2+1} (2a-2b+2c + (b-2c)(\cot(ex+d)^2+1) \right. \right. \\
& \left. \left. + 2\sqrt{a-b+c} \sqrt{(\cot(ex+d)^2+1)^2 c + (b-2c)(\cot(ex+d)^2+1) + a-b+c} \right) \right)
\end{aligned}$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot(ex+d)^3}{(a+b\cot(ex+d)^2+c\cot(ex+d)^4)^{3/2}} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$-\frac{\operatorname{arctanh}\left(\frac{2a-b+(b-2c)\cot(ex+d)^2}{2\sqrt{a-b+c}\sqrt{a+b\cot(ex+d)^2+c\cot(ex+d)^4}}\right)}{2(a-b+c)^{3/2}e} + \frac{a(b-2c)+(2a-b)c\cot(ex+d)^2}{(a-b+c)(-4ac+b^2)e\sqrt{a+b\cot(ex+d)^2+c\cot(ex+d)^4}}$$

Result (type 3, 508 leaves):

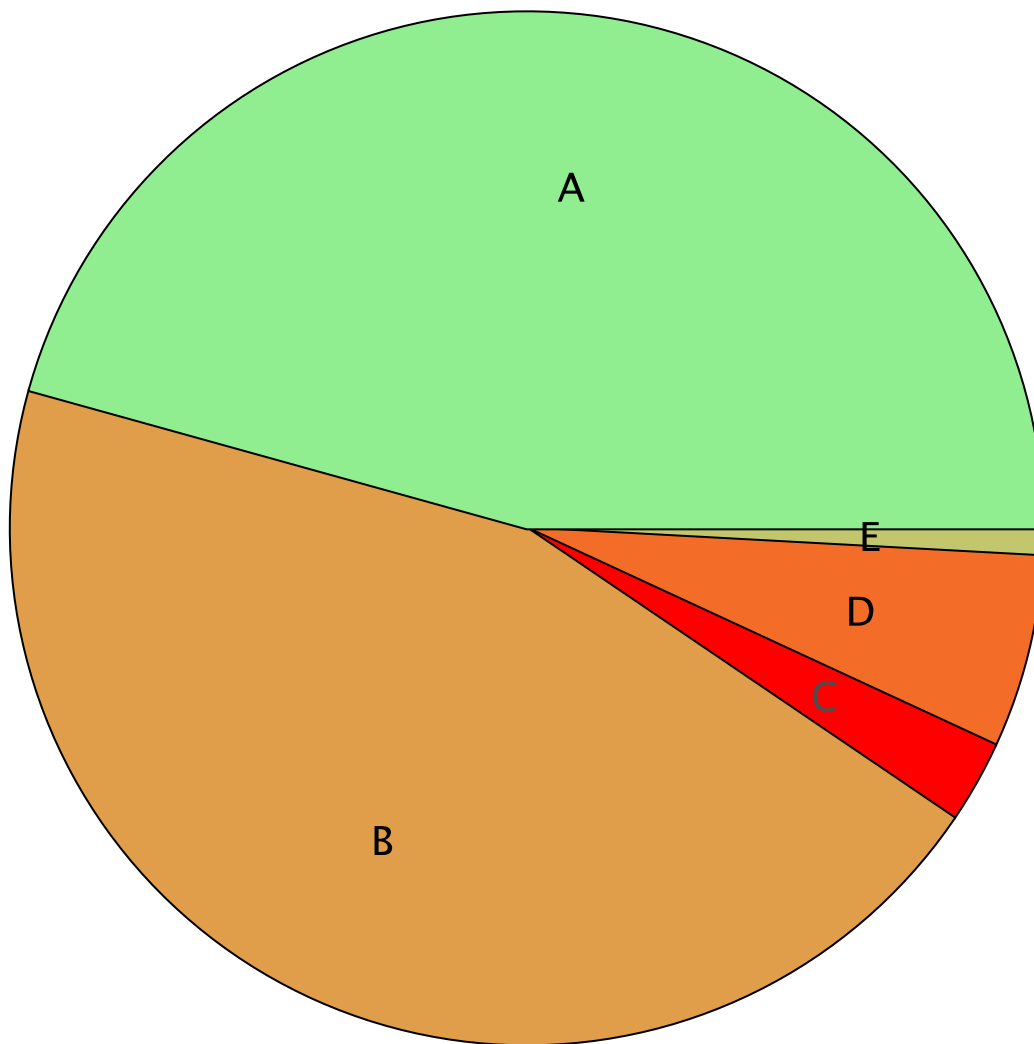
$$\begin{aligned}
& - \frac{2c\cot(ex+d)^2}{e\sqrt{a+b\cot(ex+d)^2+c\cot(ex+d)^4}(4ac-b^2)} - \frac{b}{e\sqrt{a+b\cot(ex+d)^2+c\cot(ex+d)^4}(4ac-b^2)} \\
& + \frac{2c \ln\left(\frac{2a-2b+2c+(b-2c)(\cot(ex+d)^2+1)+2\sqrt{a-b+c}\sqrt{(\cot(ex+d)^2+1)^2 c+(b-2c)(\cot(ex+d)^2+1)+a-b+c}}{\cot(ex+d)^2+1}\right)}{e(2c+\sqrt{-4ac+b^2}-b)(-2c+\sqrt{-4ac+b^2}+b)\sqrt{a-b+c}} \\
& - \frac{2c \sqrt{\left(\cot(ex+d)^2 - \frac{-b+\sqrt{-4ac+b^2}}{2c}\right)^2 c + \sqrt{-4ac+b^2} \left(\cot(ex+d)^2 - \frac{-b+\sqrt{-4ac+b^2}}{2c}\right)}}{e(-4ac+b^2)(2c+\sqrt{-4ac+b^2}-b) \left(\cot(ex+d)^2 + \frac{b}{2c} - \frac{\sqrt{-4ac+b^2}}{2c}\right)}
\end{aligned}$$



$$+ \frac{2c \sqrt{\left( \cot(ex+d)^2 + \frac{b + \sqrt{-4ac + b^2}}{2c} \right)^2 c - \sqrt{-4ac + b^2} \left( \cot(ex+d)^2 + \frac{b + \sqrt{-4ac + b^2}}{2c} \right)}}{e(-4ac + b^2) \left( -2c + \sqrt{-4ac + b^2} + b \right) \left( \cot(ex+d)^2 + \frac{b}{2c} + \frac{\sqrt{-4ac + b^2}}{2c} \right)}$$

Summary of Integration Test Results

116 integration problems



A - 53 optimal antiderivatives

- B - 52 more than twice size of optimal antiderivatives
- C - 3 unnecessarily complex antiderivatives
- D - 7 unable to integrate problems
- E - 1 integration timeouts